

# A data-driven algorithm to optimize the placement of continuous monitoring sensors on oil and gas sites

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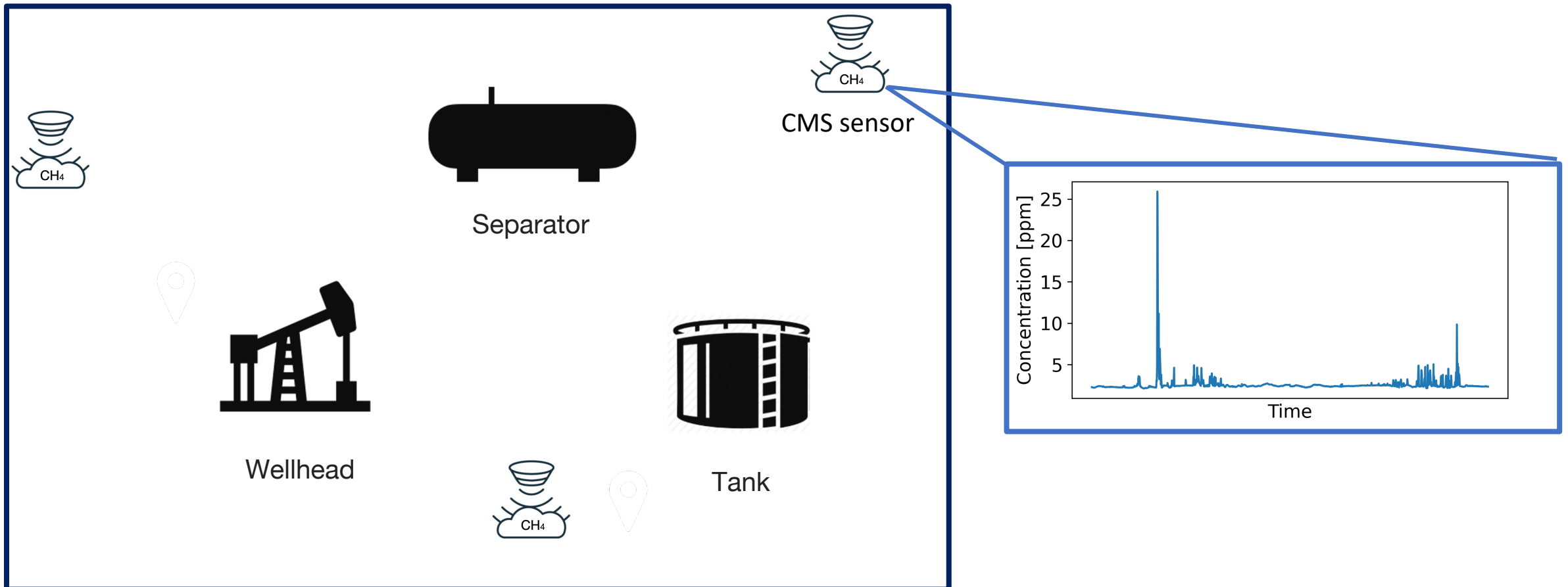
# AGU23

San Francisco, CA & Online Everywhere  
11-15 December 2023

December 11, 2023,  
San Francisco, CA

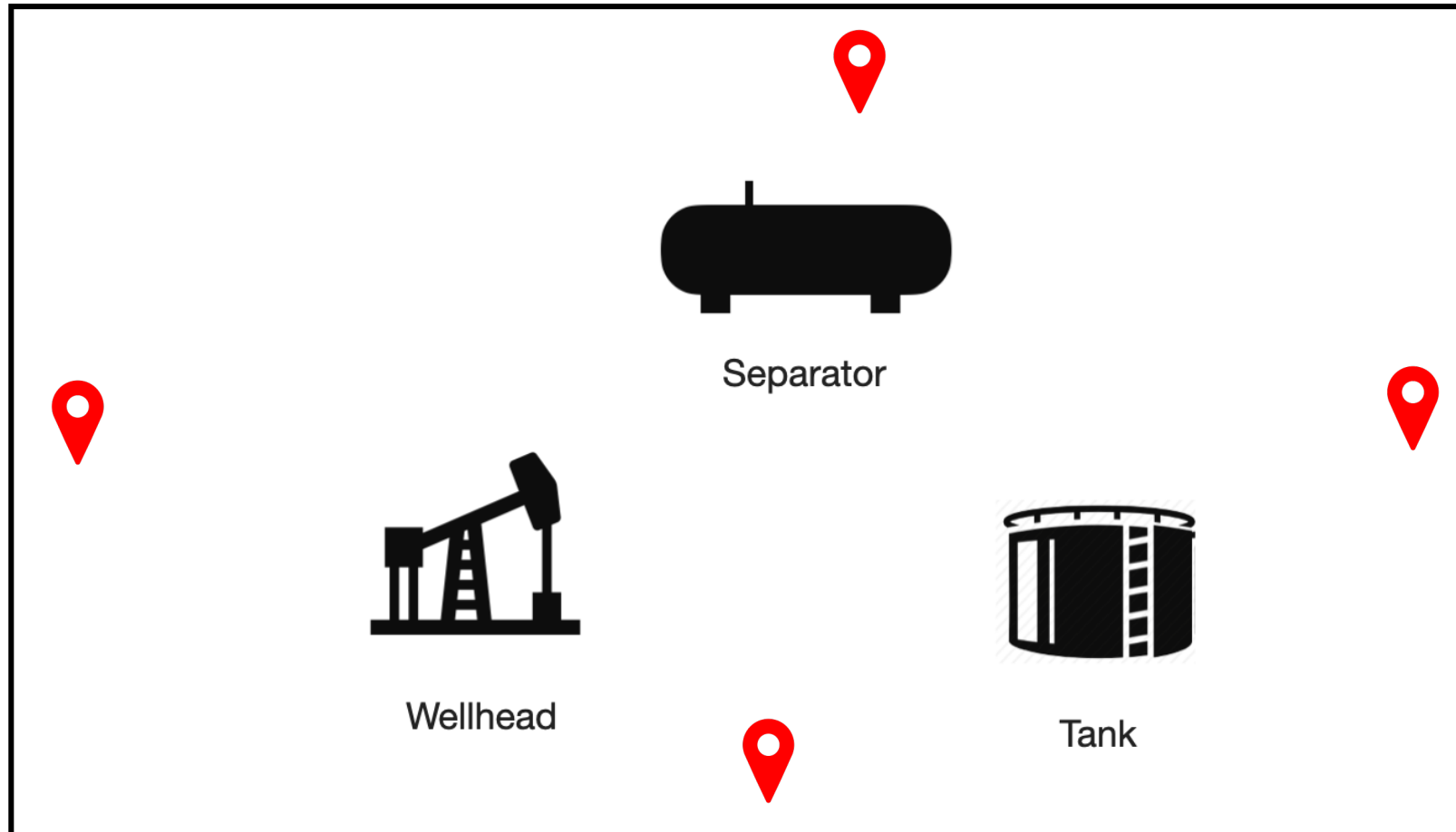
# Problem Setup

- Continuous monitoring systems (CMS)



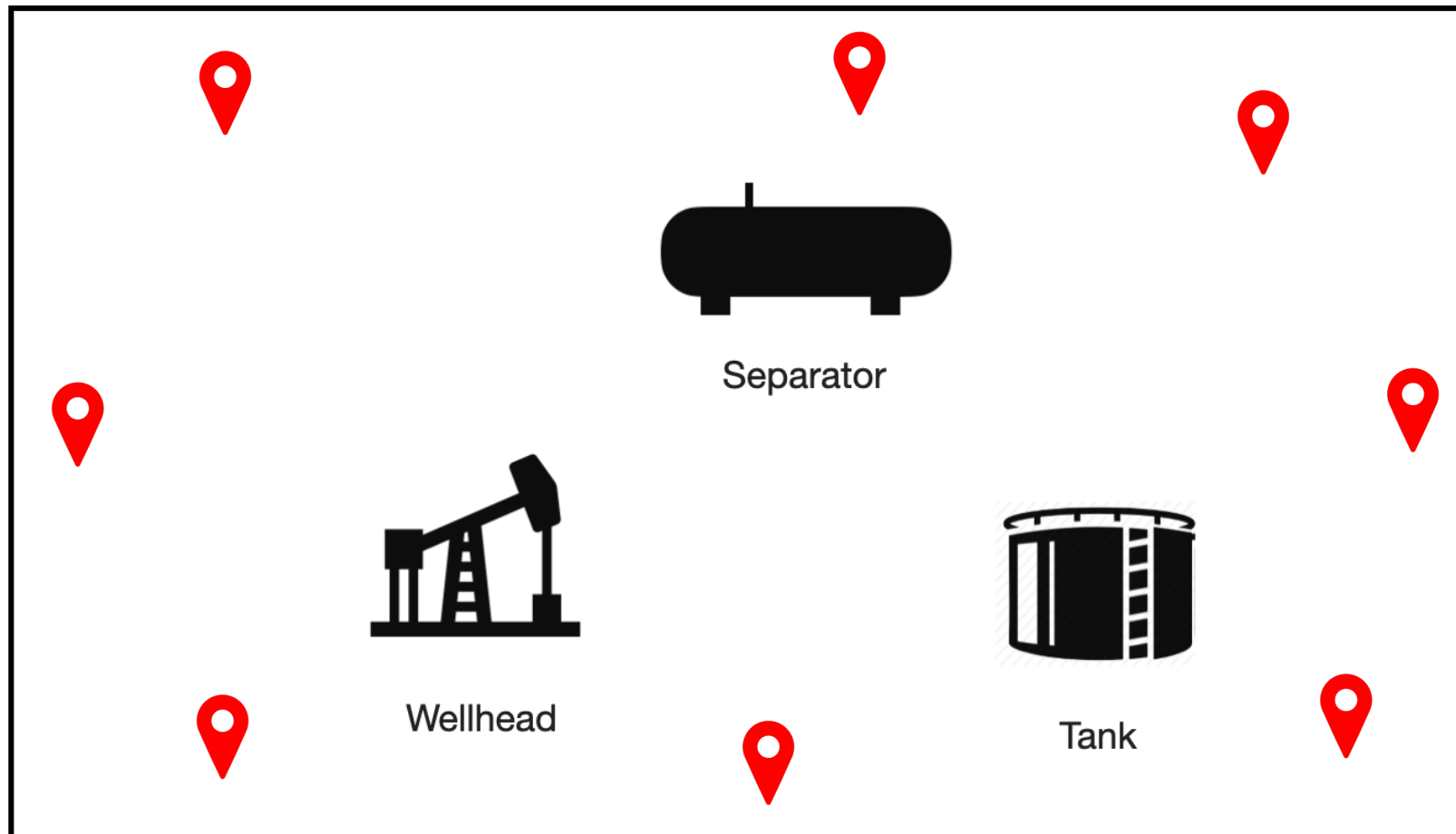
# Problem Setup

- CMS sensor placement



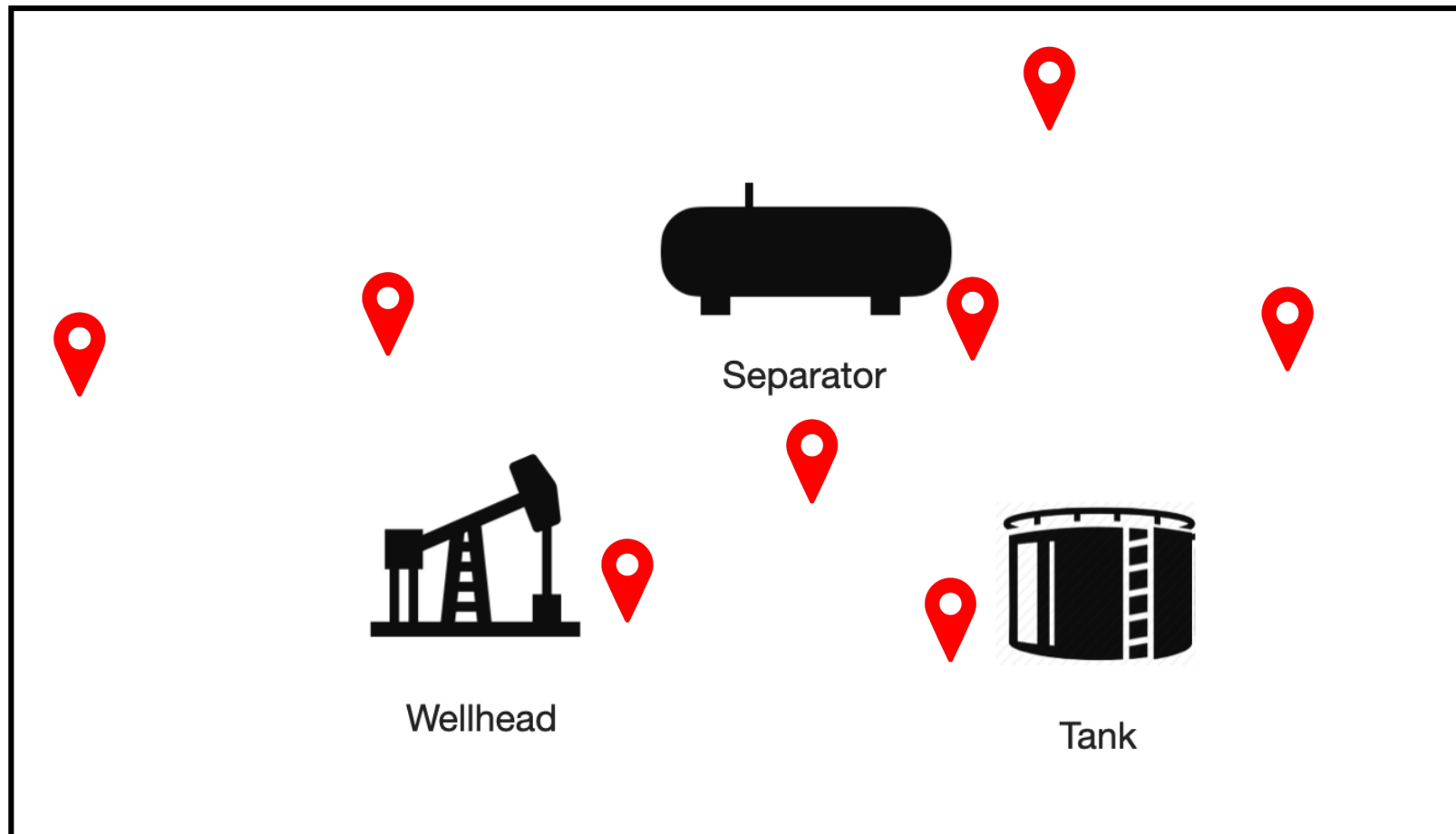
# Problem Setup

- CMS sensor placement



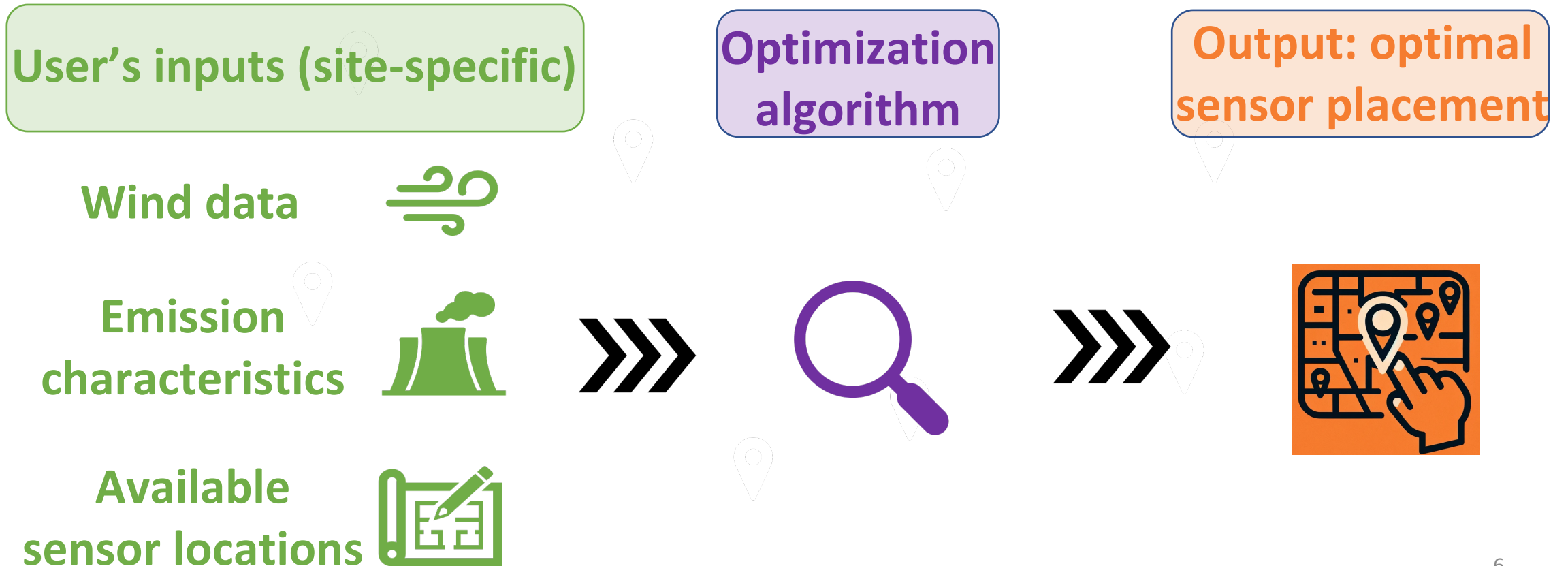
# Problem Setup

- CMS sensor placement

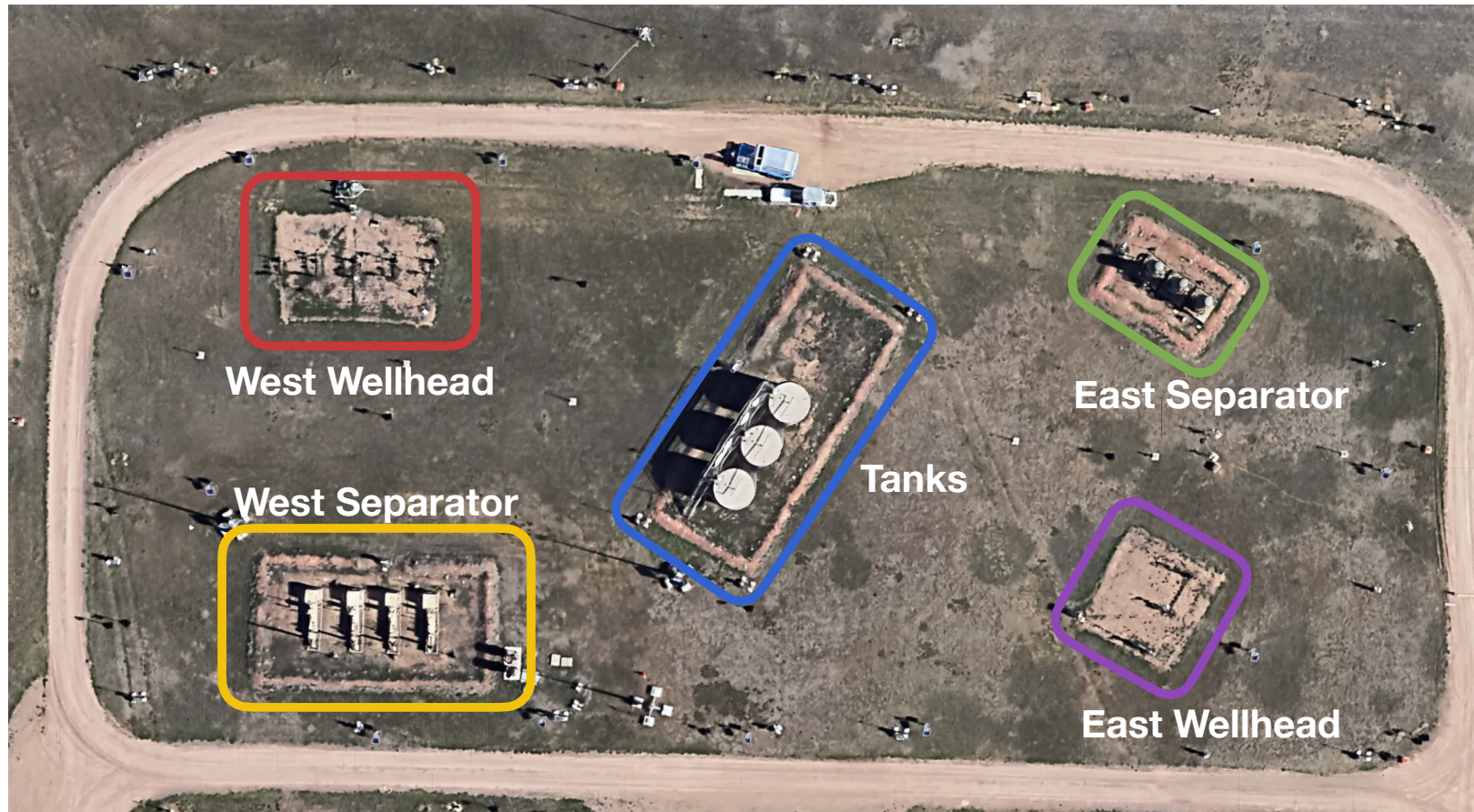


# Problem Setup

- A data-driven algorithm to optimize sensor placement for best emission detection



# Experiment Data



METEC Facility, 5 potential emission sources

# Algorithm

1 Generate emission scenarios

2 Set possible sensor locations

3 Simulate concentrations & Check detection

4 Optimize sensor placement



# Step 1 Generate Emission Scenarios

User's inputs (site-specific)

Optimization algorithm

Output: optimal sensor placement

Wind data



Emission characteristics



Available sensor locations

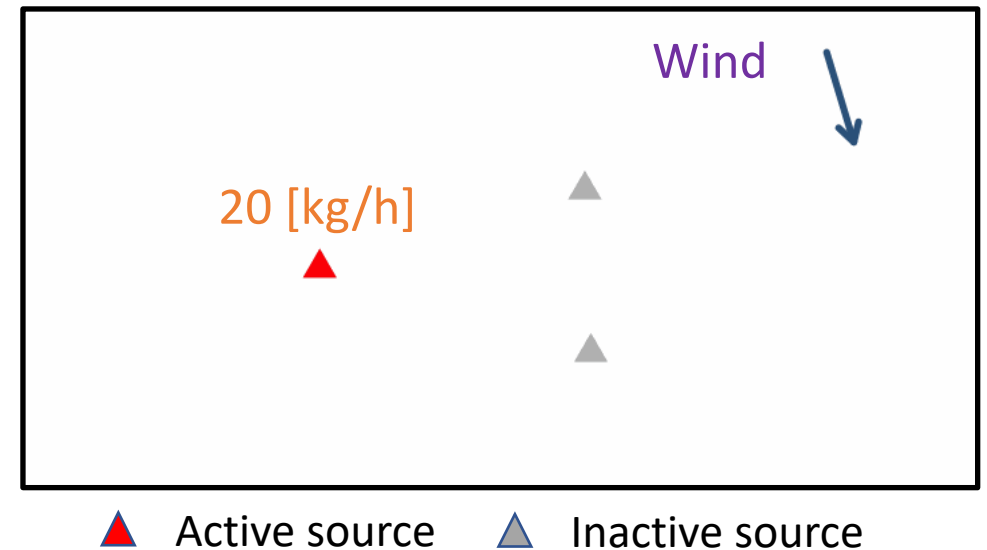


# Step 1 Generate Emission Scenarios

A combination of

- wind speed time series
- wind direction time series
- emission source location
- emission rate

defines an emission scenario.



- Estimate probability distributions of wind & emission to sample → 38,130 emission scenarios

# Step 2 Set Possible Sensor Locations

User's inputs (site-specific)

Optimization algorithm

Output: optimal sensor placement

Emission scenarios  
(# = 38,130)

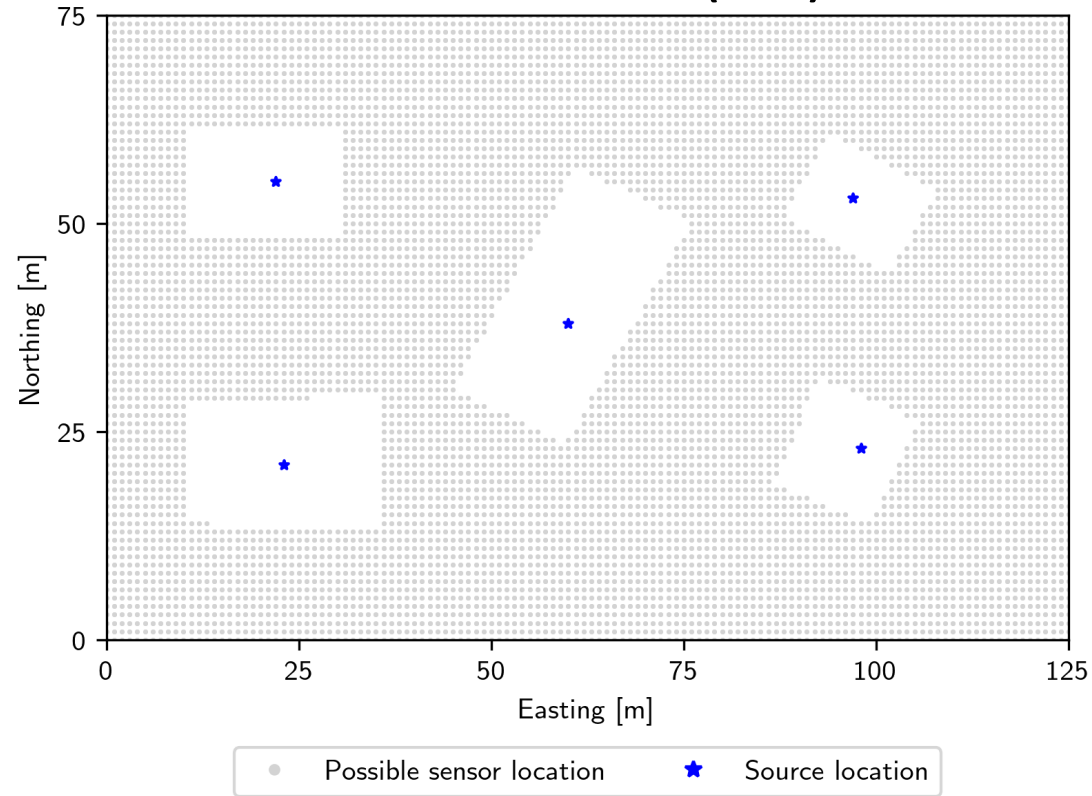


Available sensor locations

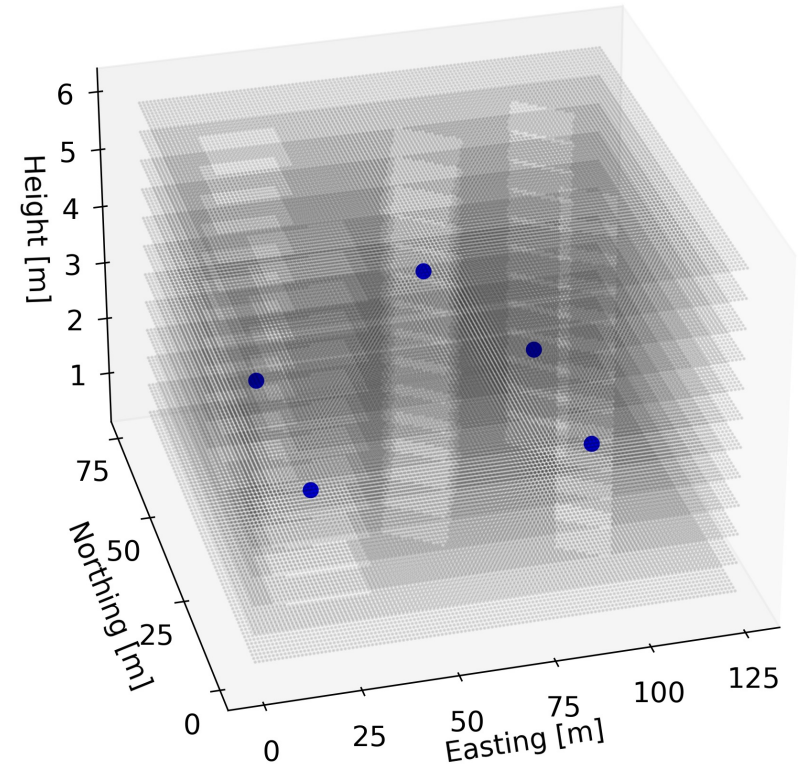


# Step 2 Possible Sensor Locations

## METEC site (2D)



## METEC site (3D)



resolution = 1 m for Northing & Easting; = 0.5 m for vertical  
# possible locations = 96,840

# Step 3 Concentration Simulation & Detection

User's inputs (site-specific)

Optimization algorithm

Output: optimal sensor placement

Emission scenarios

(# = 38,130)

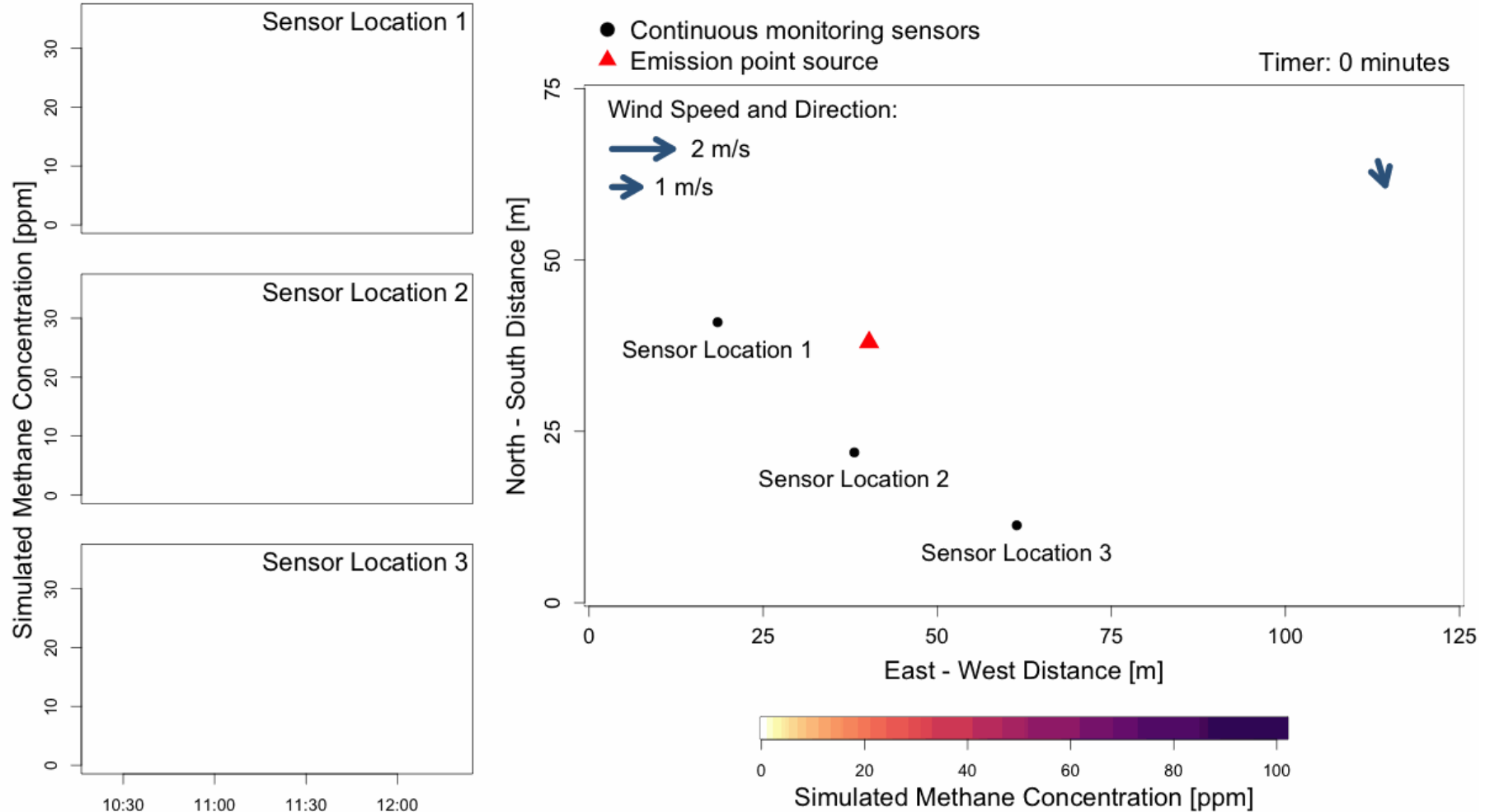


Sensor locations

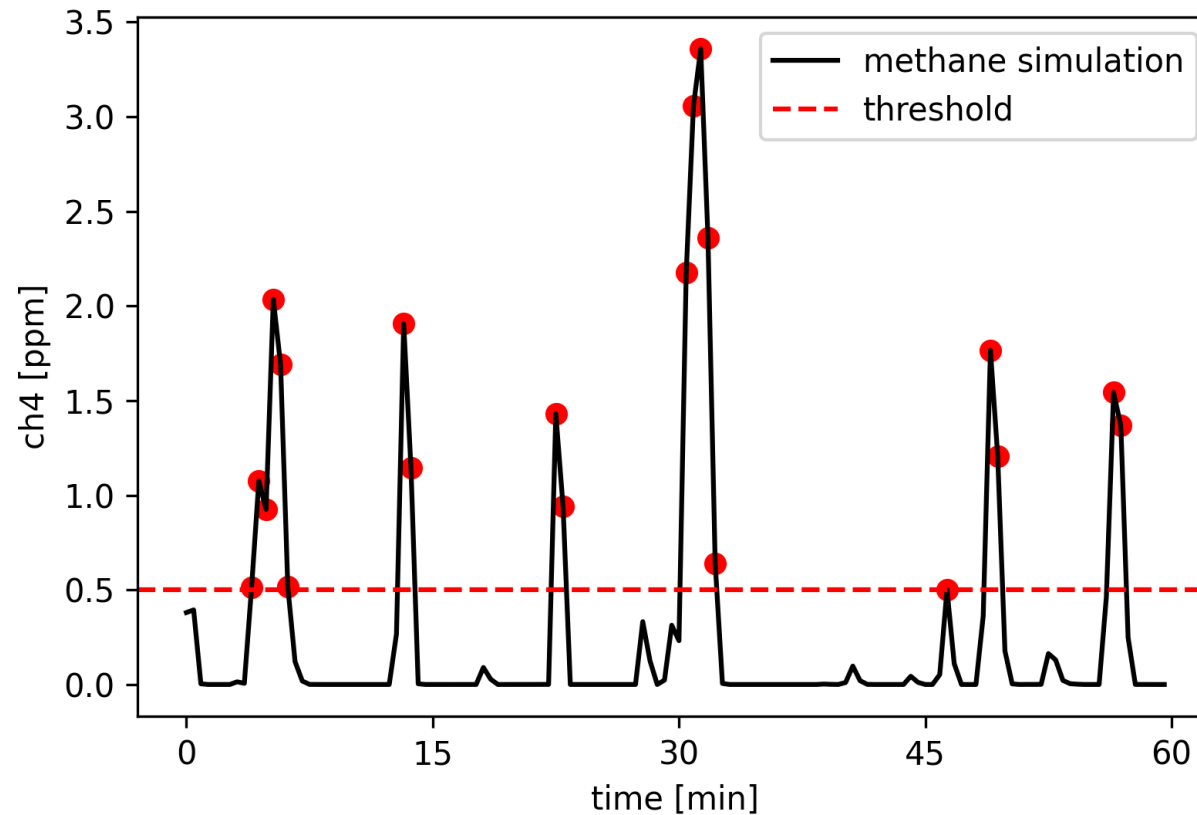
(# = 96,840)



# Step 3.1 Gaussian puff simulation

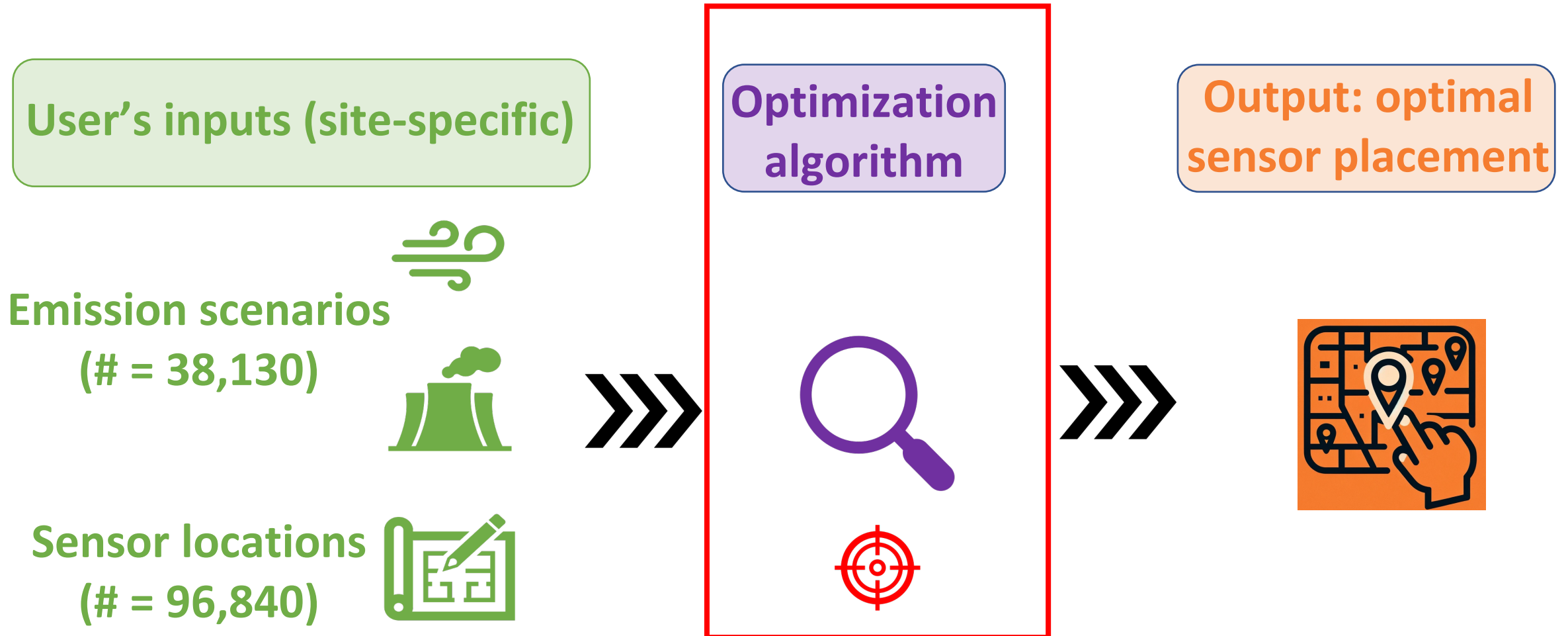


## Step 3.2 Detection



Example of simulated concentrations and detection for Emission Scenario  $j$  at Sensor Location  $i$

# Step 4 Optimize Sensor Placement





# Step 4 Optimization

Rows of  $D$ : Sensor Locations (SL)

Cols of  $D$ : Emission Scenarios (ES)

$D_{ij} = 0$ , if  $SL_i$  can detect  $ES_j$ ;

$D_{ij} = 1$ , otherwise

Evolutionary Algorithms

+

Pareto Optimization

	ES <sub>1</sub>	ES <sub>2</sub>	...	ES <sub>j</sub>	...	ES <sub>M</sub>
✓ SL <sub>1</sub>	1	1	...	0	...	1
✓ SL <sub>2</sub>	1	0	...	0	...	1
⋮	⋮	⋮	⋮	⋮	⋮	⋮
✓ SL <sub>i</sub>	0	0	...	1	...	1
⋮	⋮	⋮	⋮	⋮	⋮	⋮
SL <sub>N</sub>	1	1	...	1	...	1

Detection Matrix  $D$

$N = 96,840; M = 38,130$

# Results

User's inputs (site-specific)

Emission scenarios



Available sensor locations



Optimization algorithm

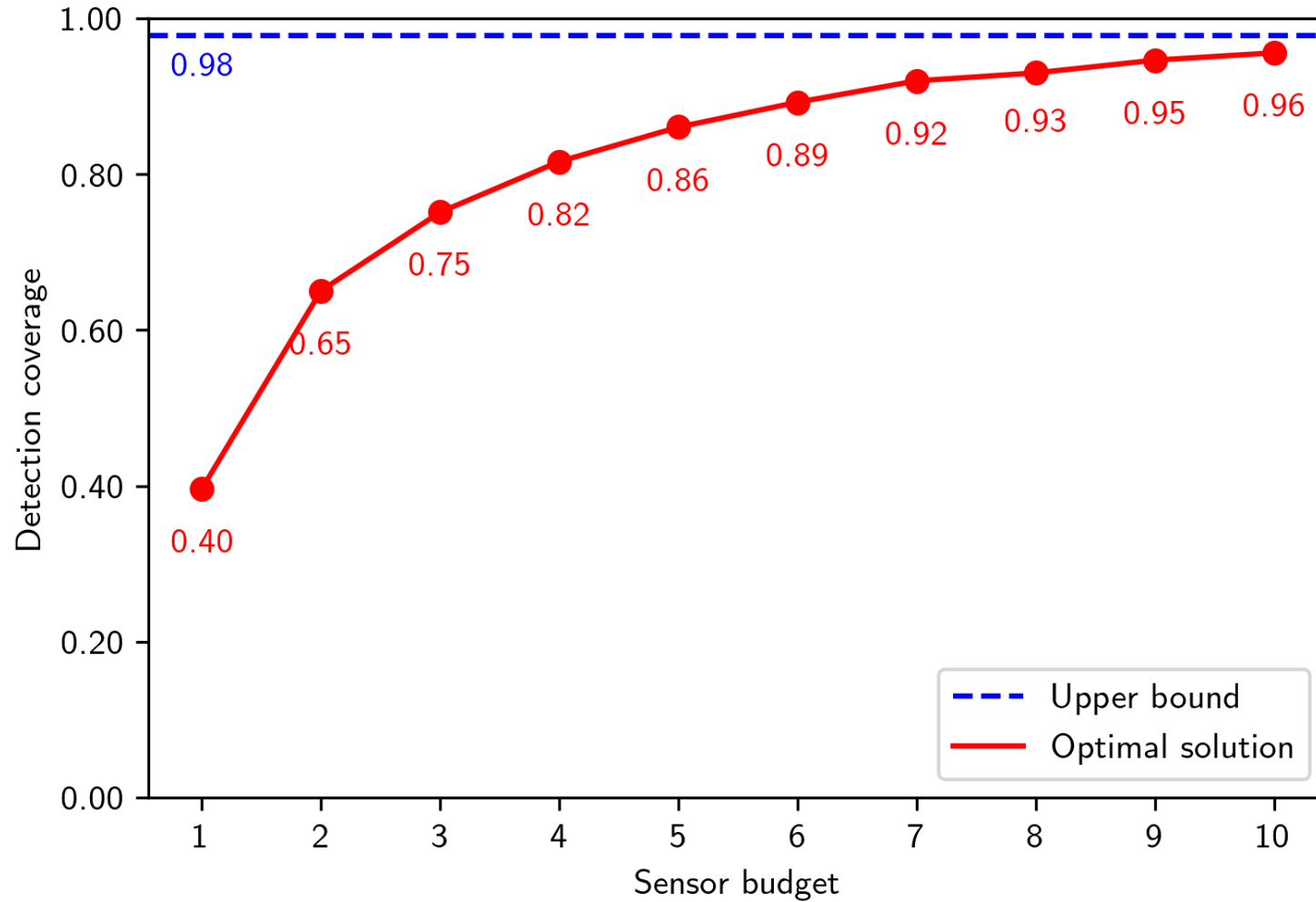


Output: optimal sensor placement





# Results: Budget vs. coverage



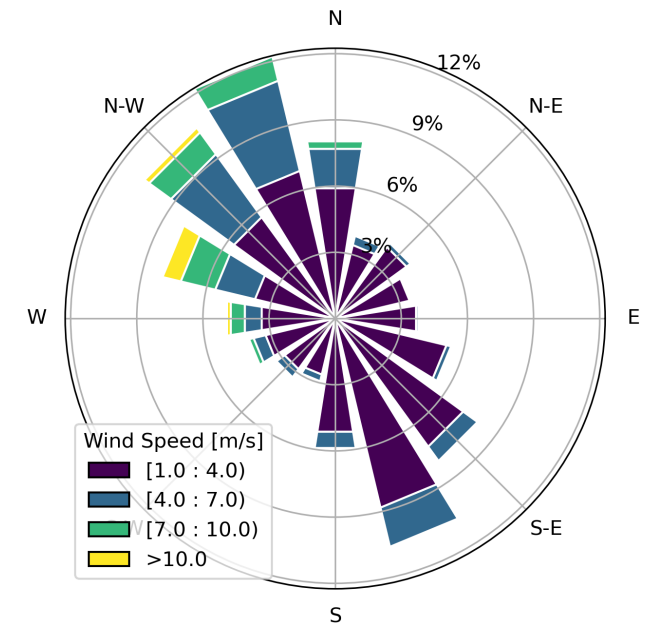
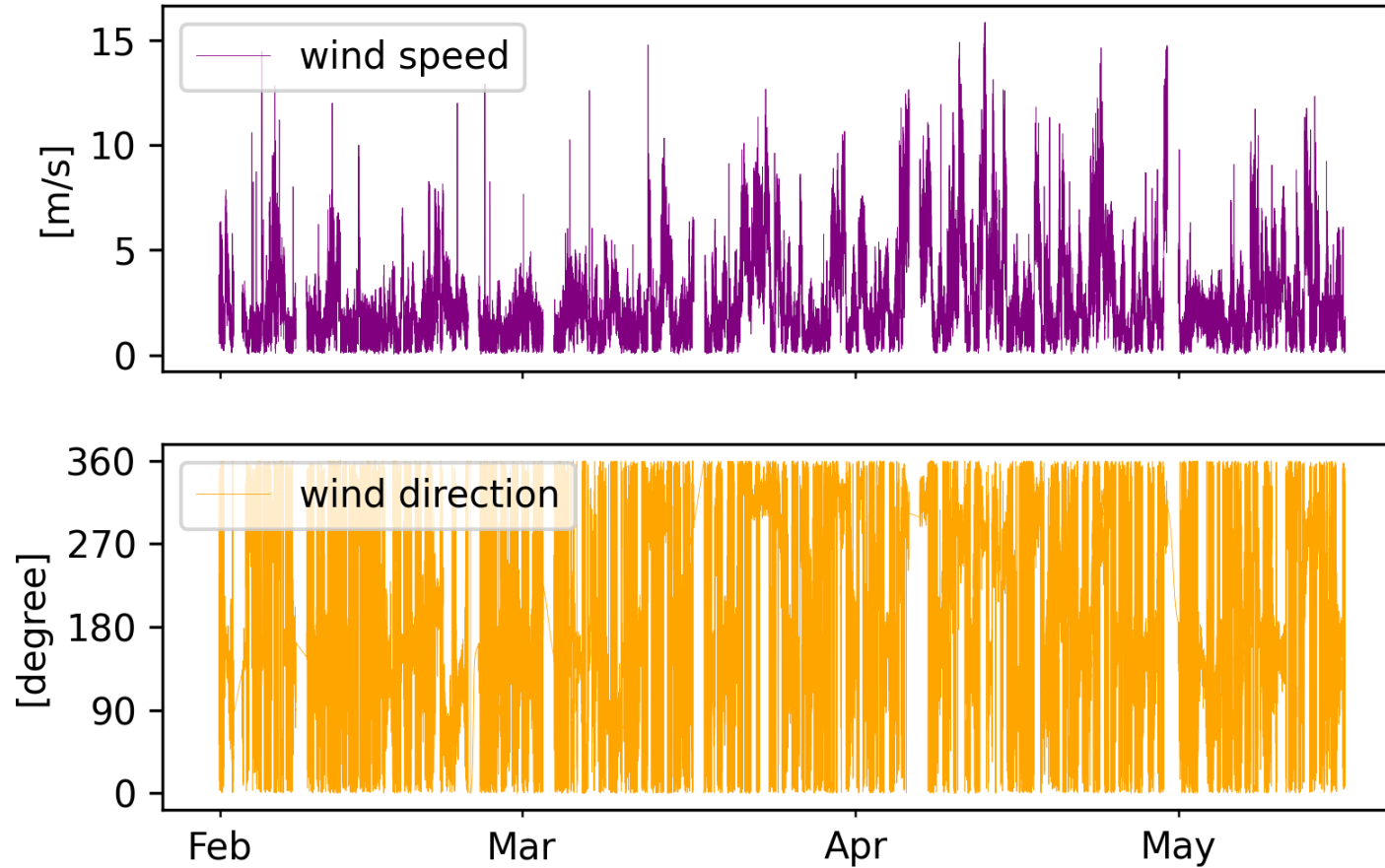
Thank you for  
attending!  
Questions?



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for more details!

Back up

# Experiment Data



Wind Data on METEC, February through May 2022

# Step 4.2 Pareto Optimization & EA

## Pareto Optimization

### Objectives:

Find a subset of rows (a solution) from the detection matrix to

- maximize emission scenario coverage.
- minimize the size of the subset.

Exhaustive search and standard linear programming algorithms are impossible for large-scale problem!

## Evolutionary Algorithms

### Process:

1. Randomly initialize a population of solutions.
2. Propose new solutions by perturbing existing solutions.
3. Update the population by eliminating worse solutions.
4. Repeat Step 2 & 3 until converge.
5. Return the best  $k$ -size solution.



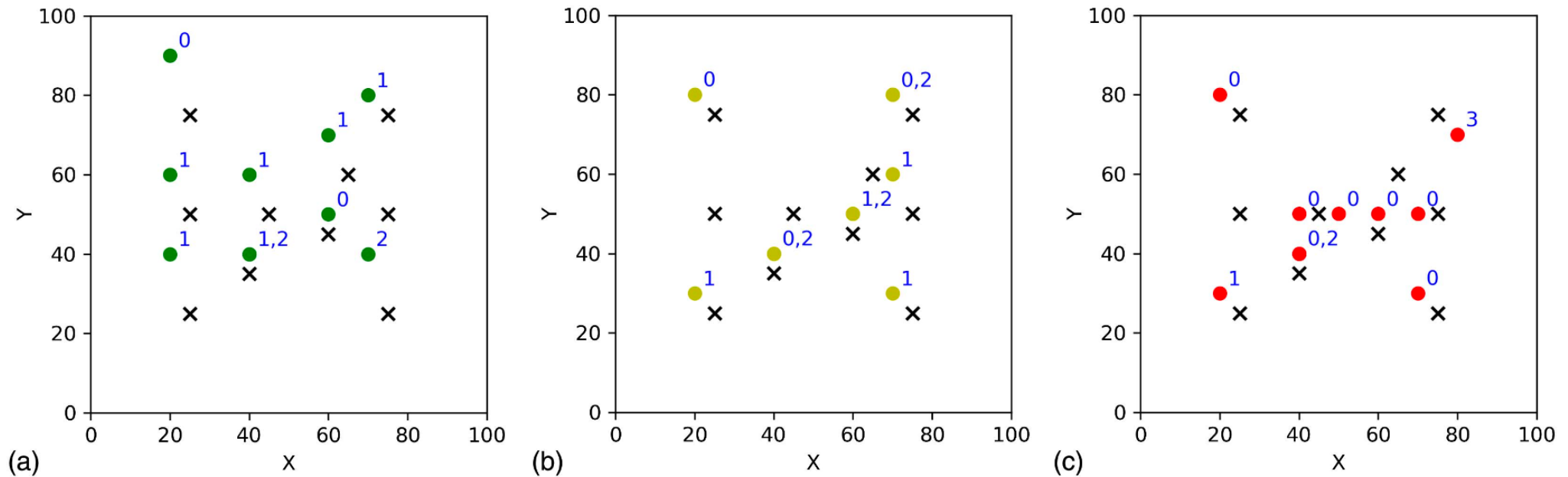
# Conclusions & Future Work

- Developed a data-driven algorithm for sensor placement more accurate and efficient than traditional methods.
- The algorithm's modularity ensures adaptability to various monitoring needs.
- Optimized for solving large-scale problems efficiently.
- To implement a generative model for better approximation of wind distributions, thereby expanding the emission scenario database.
- To investigate advanced data embedding techniques to manage and solve problems of greater scale.

# References

- Klise, Katherine A., et al. "Sensor placement optimization software applied to site-scale methane-emissions monitoring." *Journal of Environmental Engineering* 146.7 (2020): 04020054.
- Qian, Chao, Chao Bian, and Chao Feng. "Subset selection by pareto optimization with recombination." *Proceedings of the AAAI Conference on Artificial Intelligence*. Vol. 34. No. 03. 2020.

# Close sensor locations

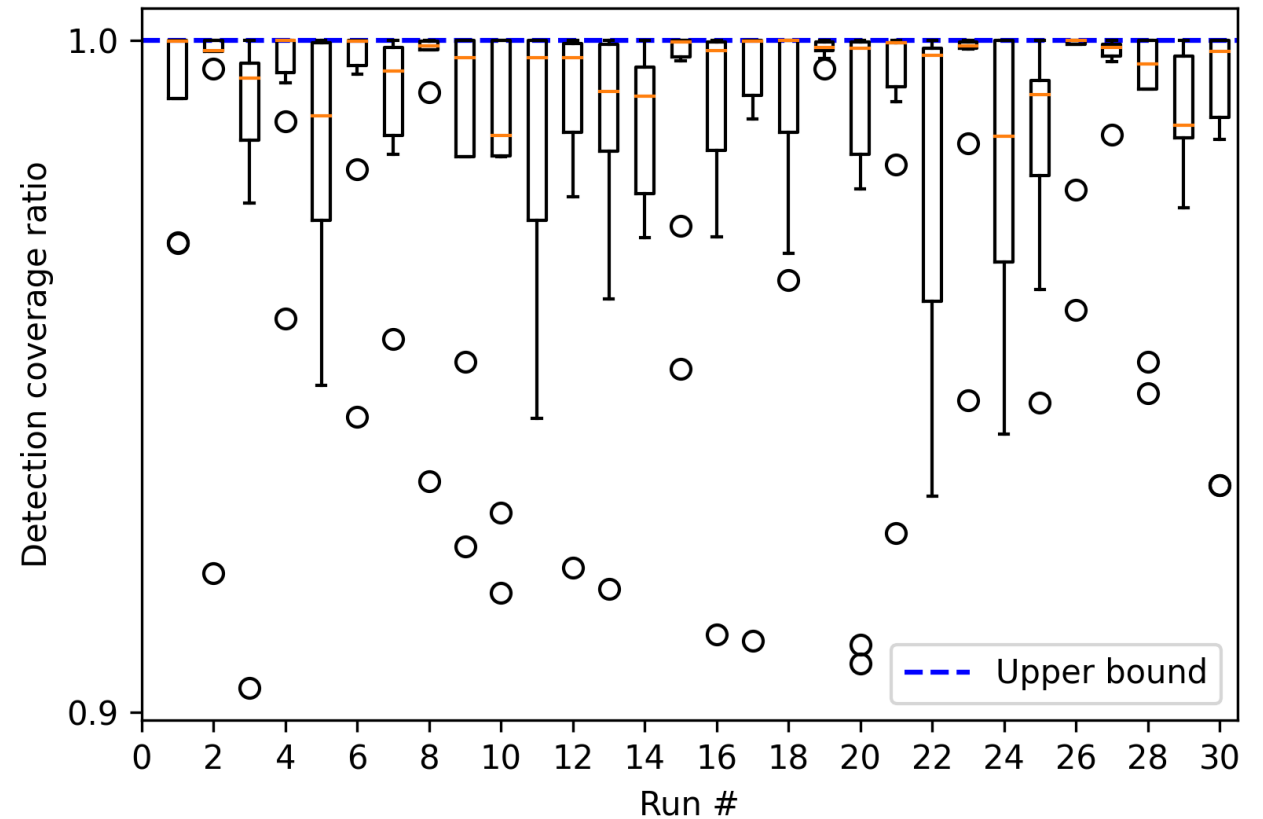


**Fig. 9.** Optimal sensor placements with 10 sensors maximizing scenario coverage considering (a) high-sensitivity; (b) moderate-sensitivity; and (c) low-sensitivity sensors. X's represent the potential leak locations. The height of each sensor is noted (some sensors overlap in plan-view).

Figure 9 in Klise et al. (2020)

# Test EA on synthetic large matrix

- $nrows = ncols = 100,000$
- $k = 10$ , randomly placement in the big matrix
- Test on 30 cases and run 10 EA algorithm for each case



# Optimality Guarantee

- In theory, we prove that for subset selection with monotone objective functions, PORSS can achieve the optimal polynomial-time approximation guarantee,  $1 - e^{-\gamma}$  where  $\gamma$  is the submodularity ratio measuring how close your objective function is to submodularity.

# Related Work

	Klise et al. (2020)	Our work
# emission scenarios	1,200	≈ 40,000
# possible sensor locations	≈ 2,500	≈ 100,000
Forward model	Gaussian plume	Gaussian puff
Optimization algorithm	Mixed-integer linear programming	Pareto optimization using evolutionary algorithm (EA)

# Pareto Optimization Algorithm

- General subset selection problem

Given all items  $V = \{v_i\}, i = 1, 2, \dots, N$ , an objective function  $g$  and a budget  $k$ , to find a subset of at most  $k$  items maximizing  $g$ , i.e.,

$$\operatorname{argmax}_{S \subseteq V} g(S) \text{ s.t. } |S| \leq k$$

- In our case,  $V$  is the set of rows of the detection matrix  $D$
- $g$  is the number of 0s in the column product of  $D^S$  (the  $k$ -row submatrix of  $D$ )

# Pareto Optimization Algorithm

- Pareto Optimization
  - Find optimal solutions to two conflicting objectives

$$\operatorname{argmax}_{x \subseteq \{0,1\}^N} (g_1(x), g_2(x))$$

where

$$g_1(x) = \begin{cases} -\infty, & |x| \geq 2k \\ g(x), & \text{otherwise} \end{cases} \quad g_2(x) = -|x|$$



## Algorithm

**Input:** detection matrix  $D$ ; objective function  $g$ ; budget  $k$

**Parameters:** the number  $I$  of iterations

**Output:** a subset of  $k$  rows of  $D$

**Process:**

Let  $x = \{0\}^N$ ,  $P = \{x\}$  and  $t = 0$

**While**  $t < T$ :

Select  $x, y$  from  $P$  randomly with replacement

Apply recombination on  $x, y$  to generate  $x', y'$

Apply bit-wise mutation on  $x', y'$  to generate  $x'', y''$

**for** each  $z \in \{x'', y''\}$ :

**if**  $\nexists u \in P$  such that  $u \succ z$ :

$$P = (P \setminus \{u \in P \mid u \prec z\}) \cup \{z\}$$

Check early stop

$t = t + 1$

**return**  $\operatorname{argmax}_{x \in P, |x| \leq k} g(x)$

$$u \succ z \Leftrightarrow$$

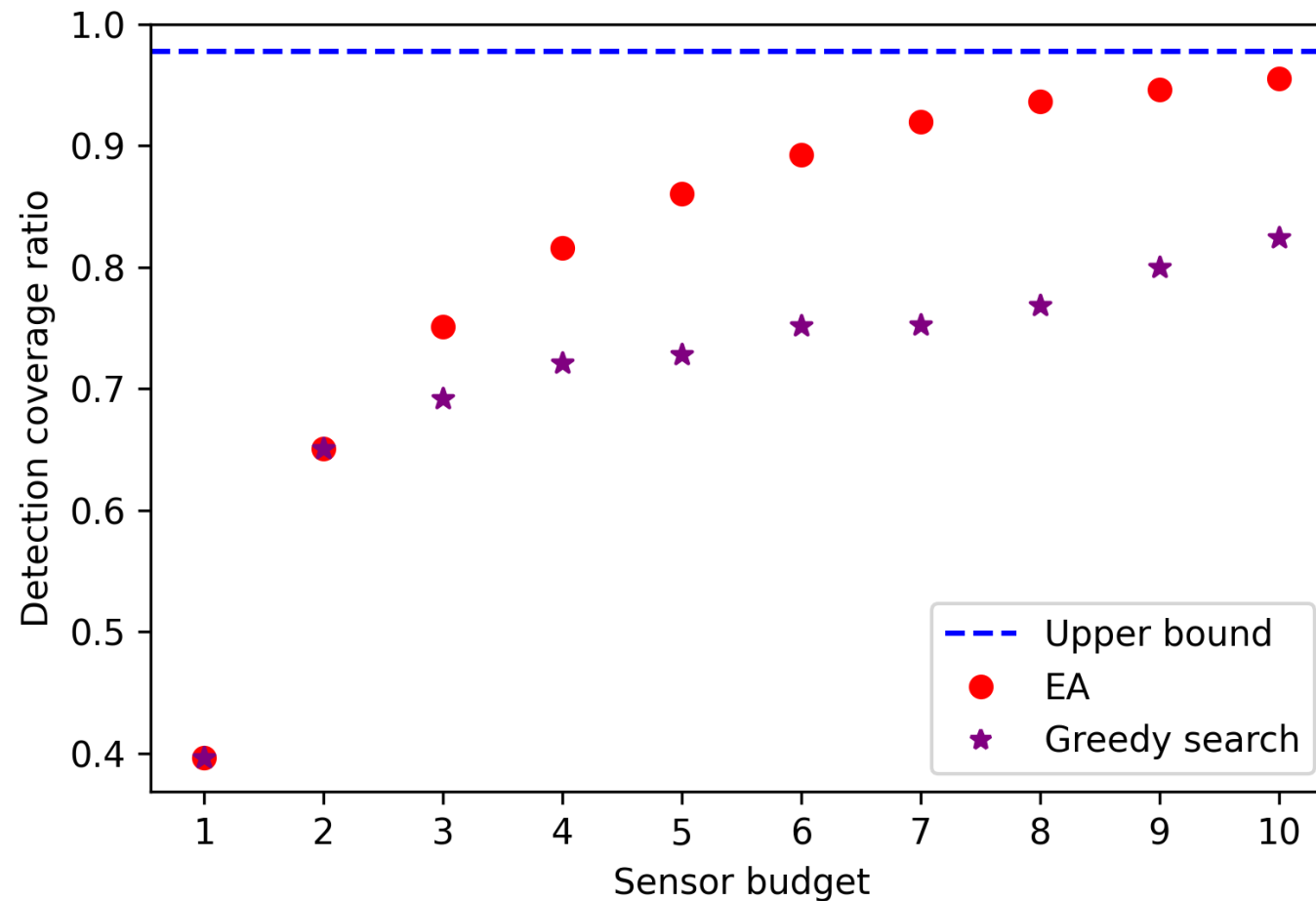
$$g_1(u) > g_1(z) \ \& \ g_2(u) \geq g_2(z)$$

or

$$g_1(u) \geq g_1(z) \ \& \ g_2(u) > g_2(z)$$

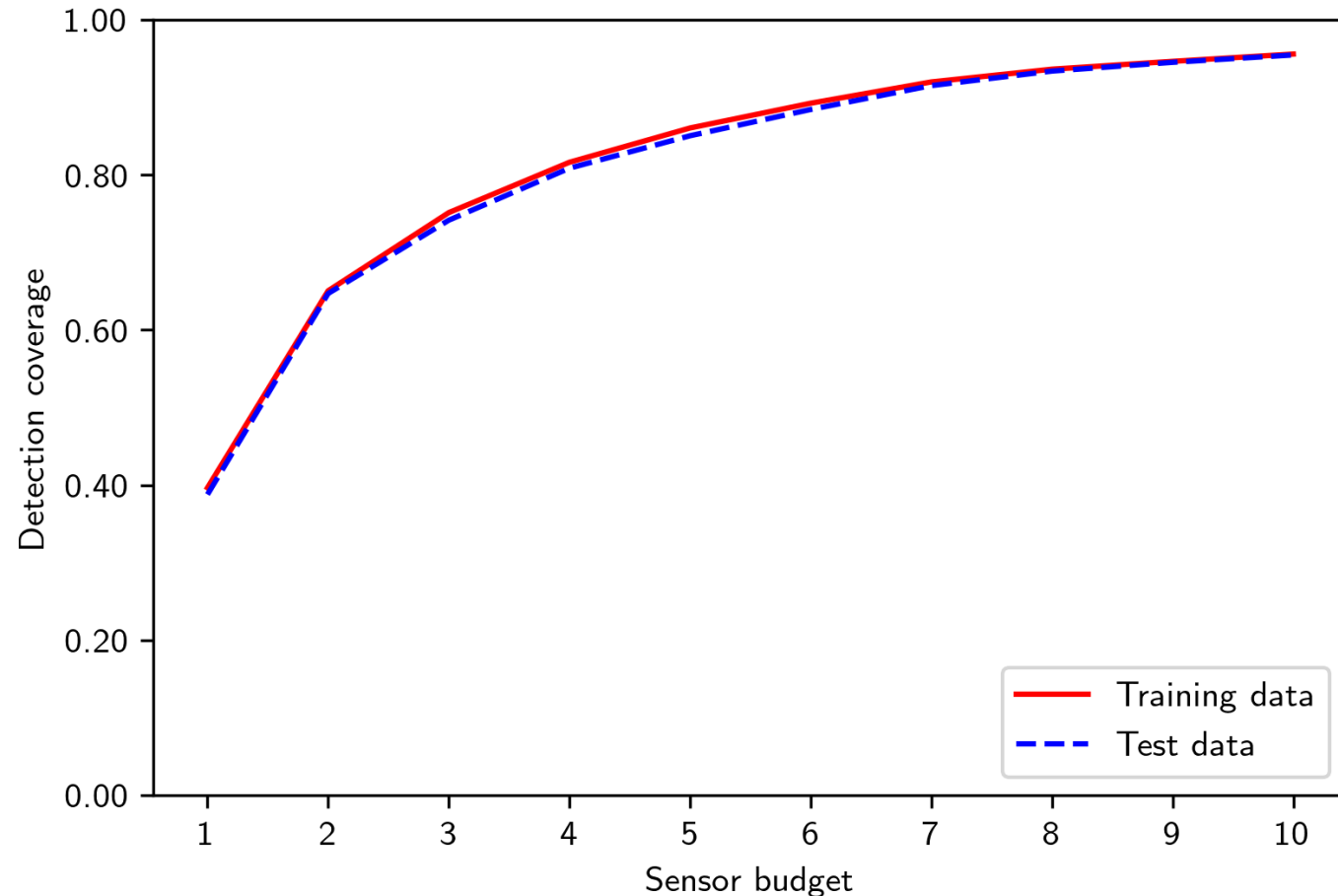
# EA vs. Greedy Search

- EA vs. greedy search

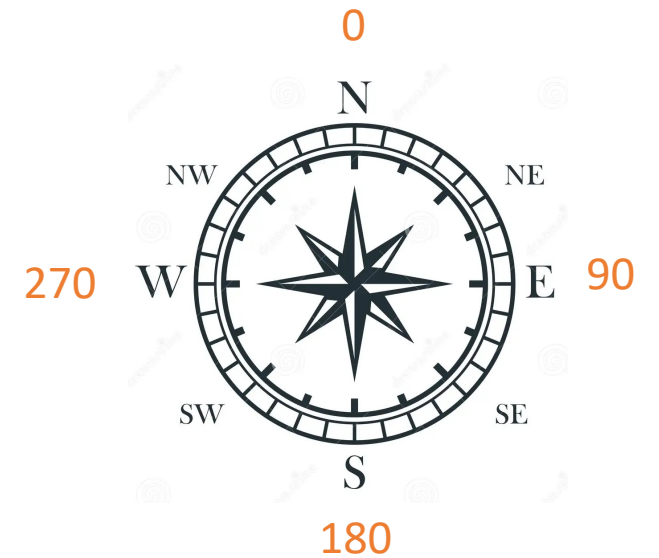
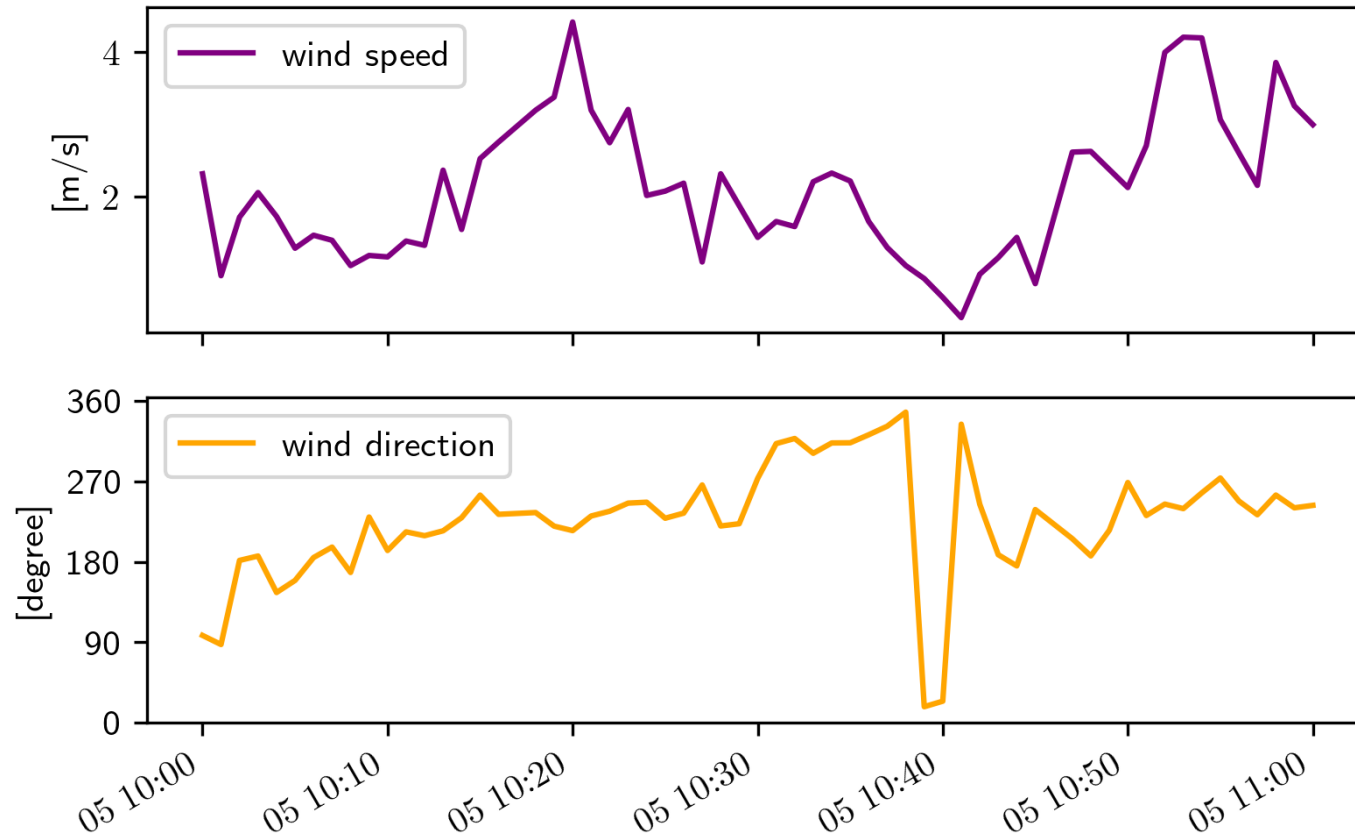


# Experiments & Results - robustness

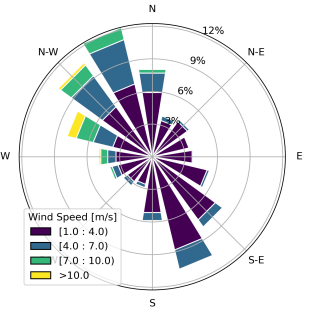
Use a different set of 10,000 emission scenarios to validate the performance of the optimal sensor placement.



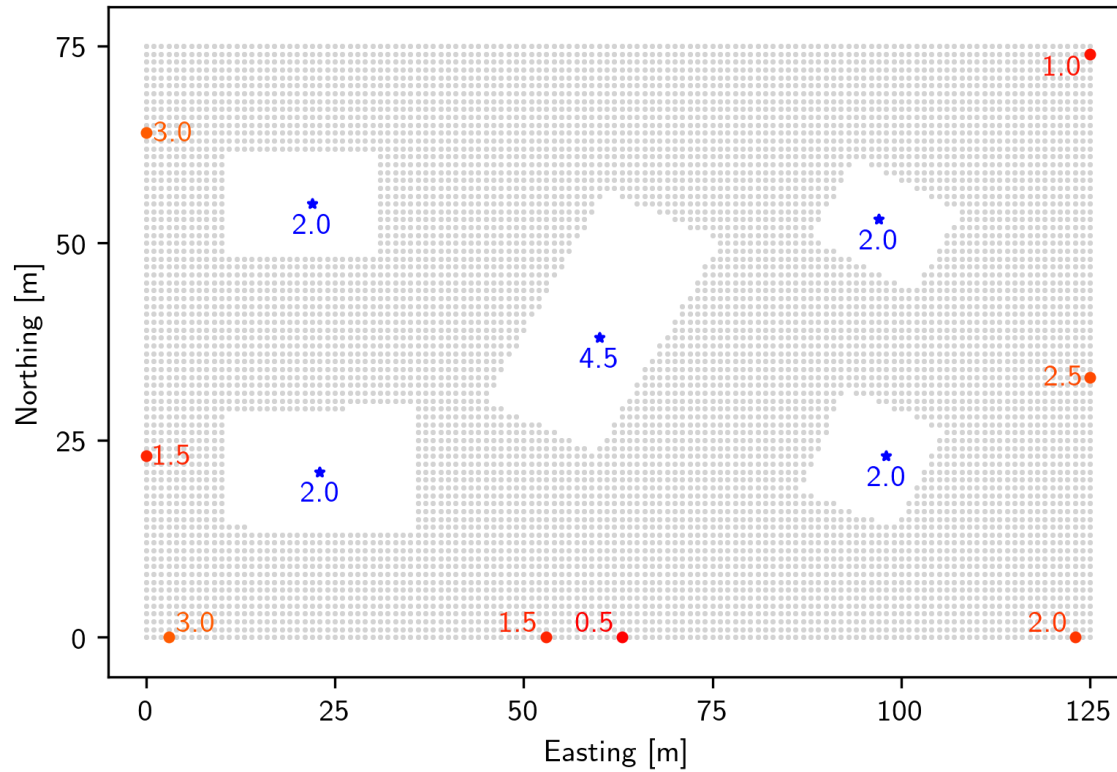
# Why some scenarios are always undetected?



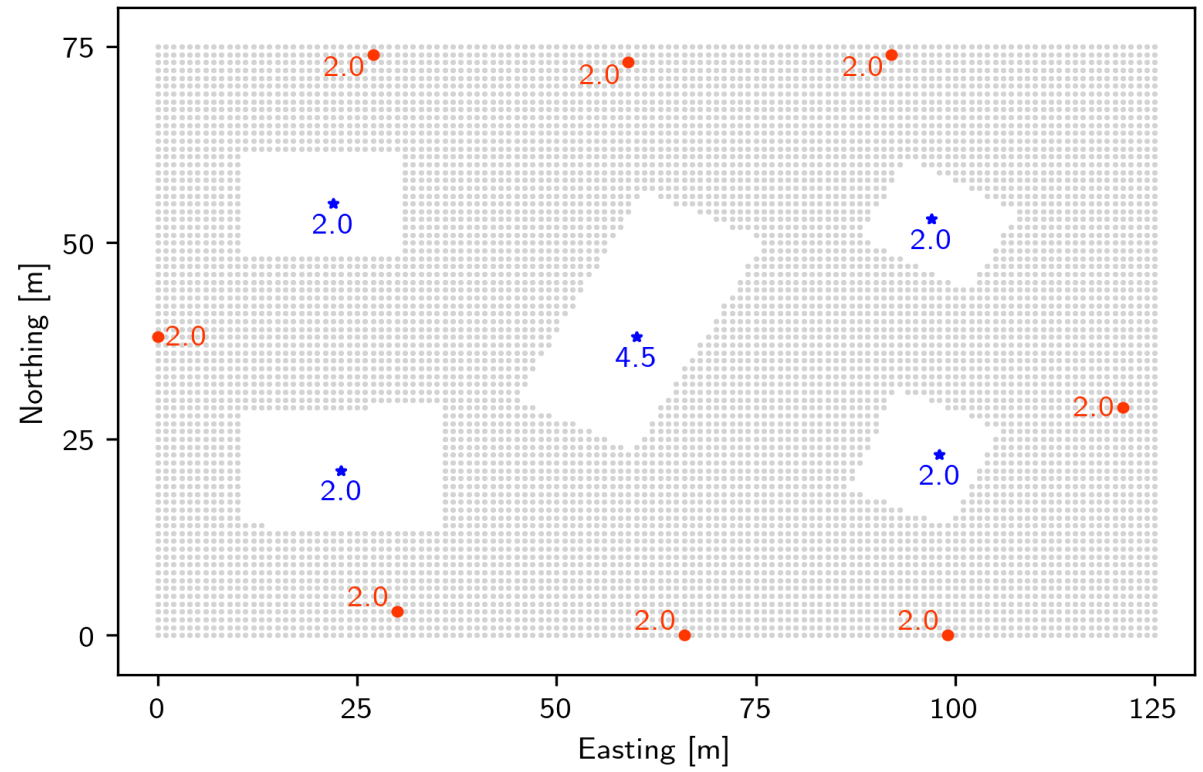
# Experiments & Results – fence line placement



Best fence line 8-sensor placement, coverage ratio = 0.83



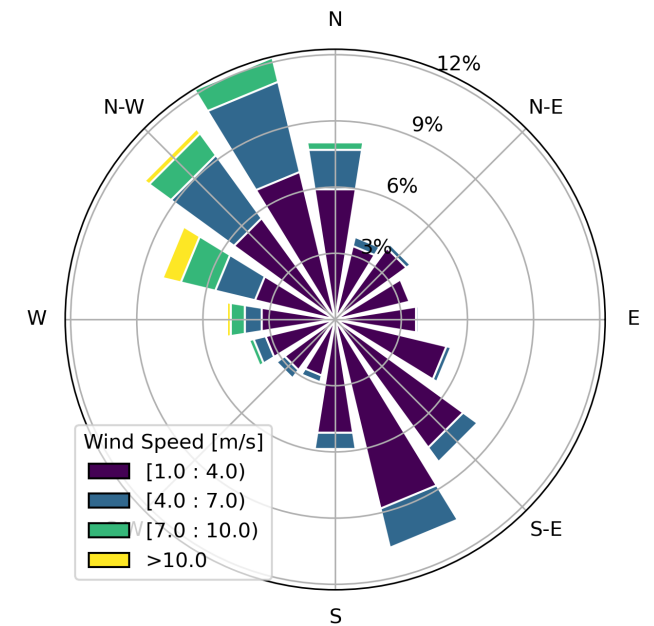
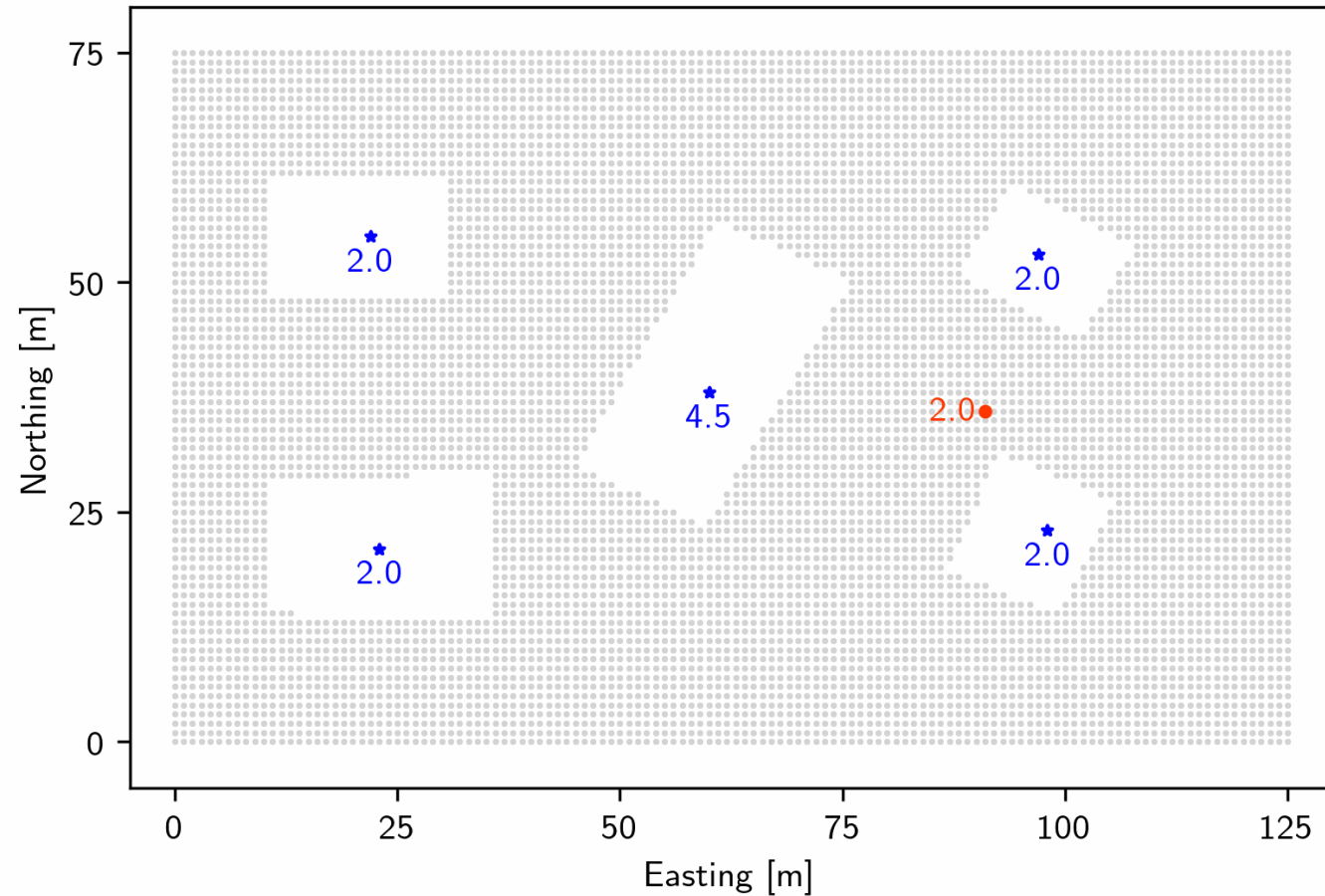
Uniform fence line 8-sensor placement, coverage ratio = 0.76



- Possible sensor location
- Selected sensor location
- ★ Source location

# Results: Best $k$ -sensor placement

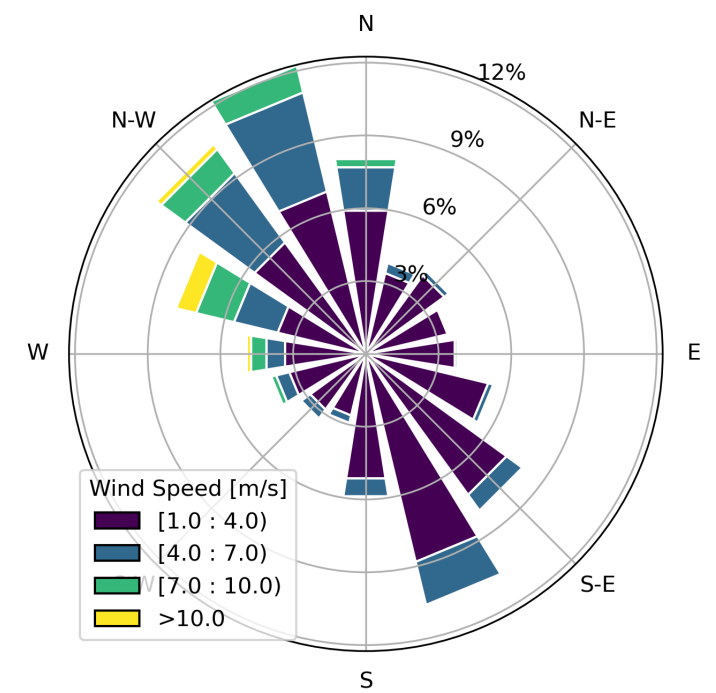
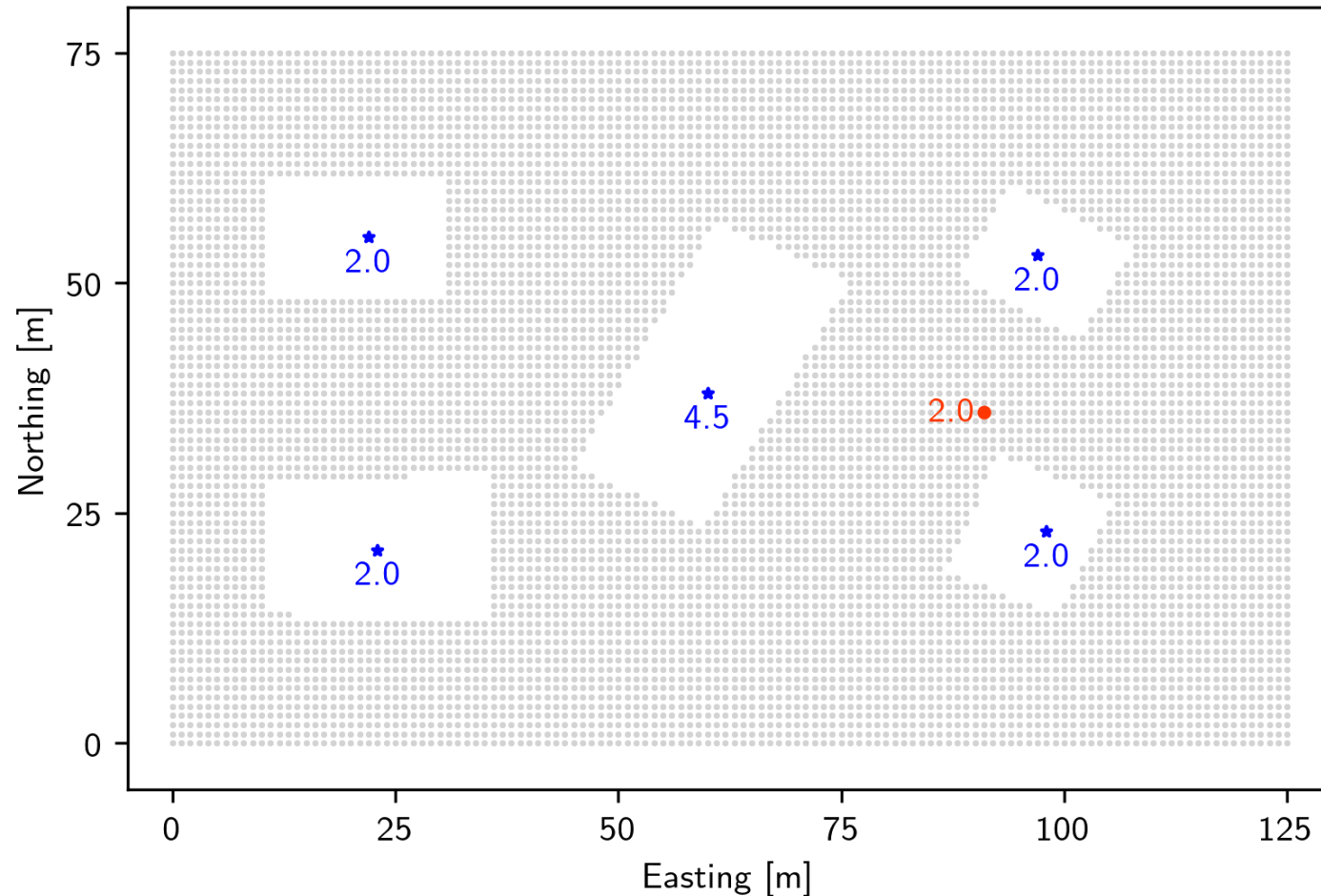
Best-1 sensor placement, coverage ratio = 0.40



- Possible sensor location
- Selected sensor location
- ★ Source location

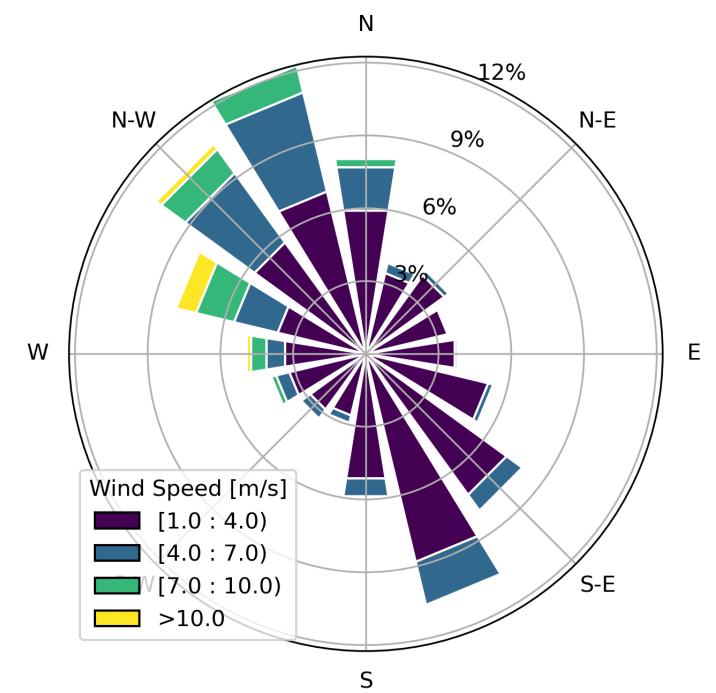
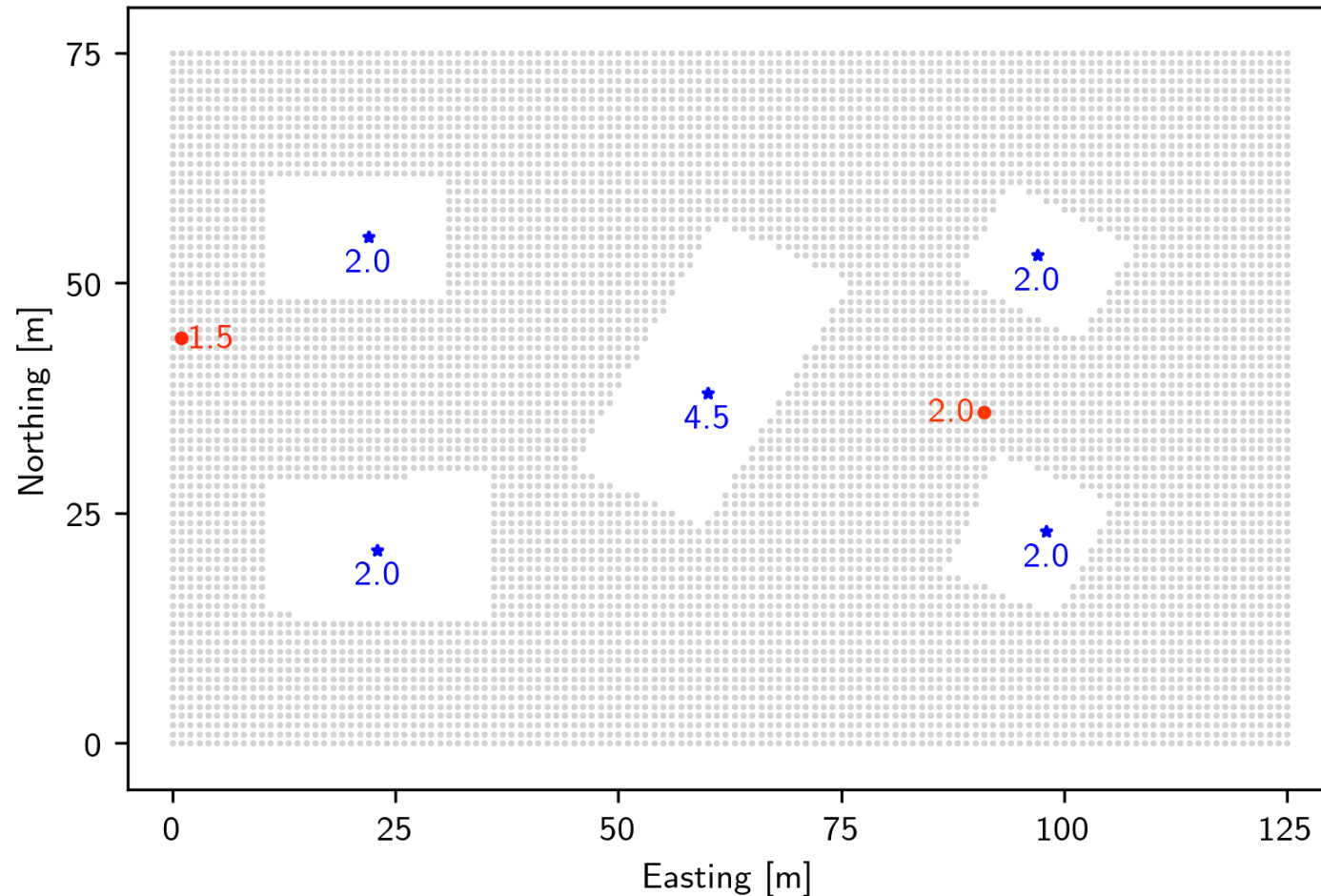
# Best-1 Sensor Placement

Best-1 sensor placement, coverage ratio = 0.40



# Best-2 Sensor Placement

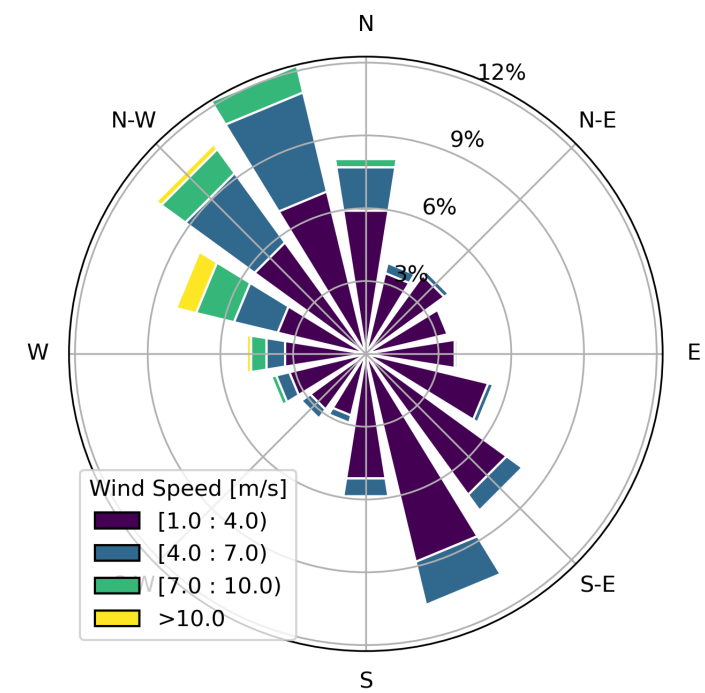
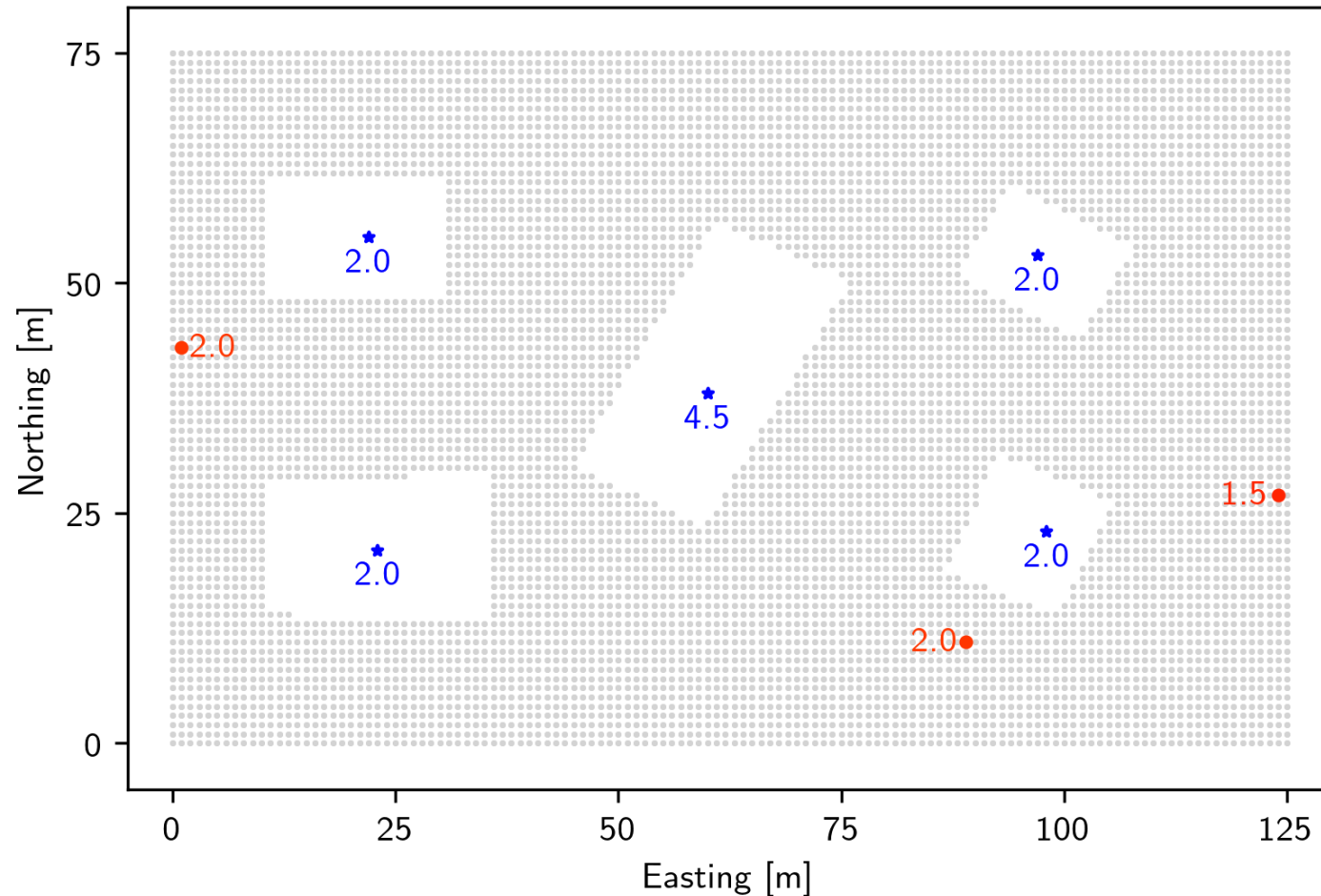
Best-2 sensor placement, coverage ratio = 0.65





# Best-3 Sensor Placement

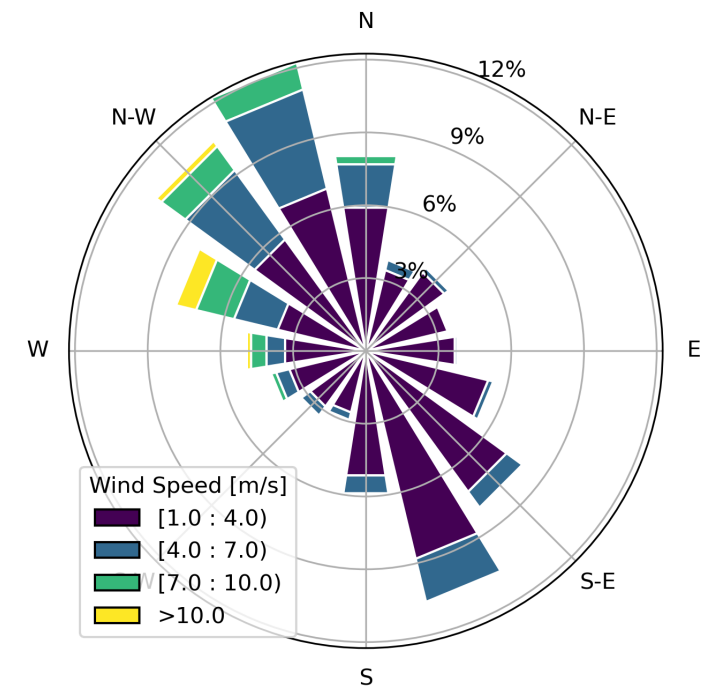
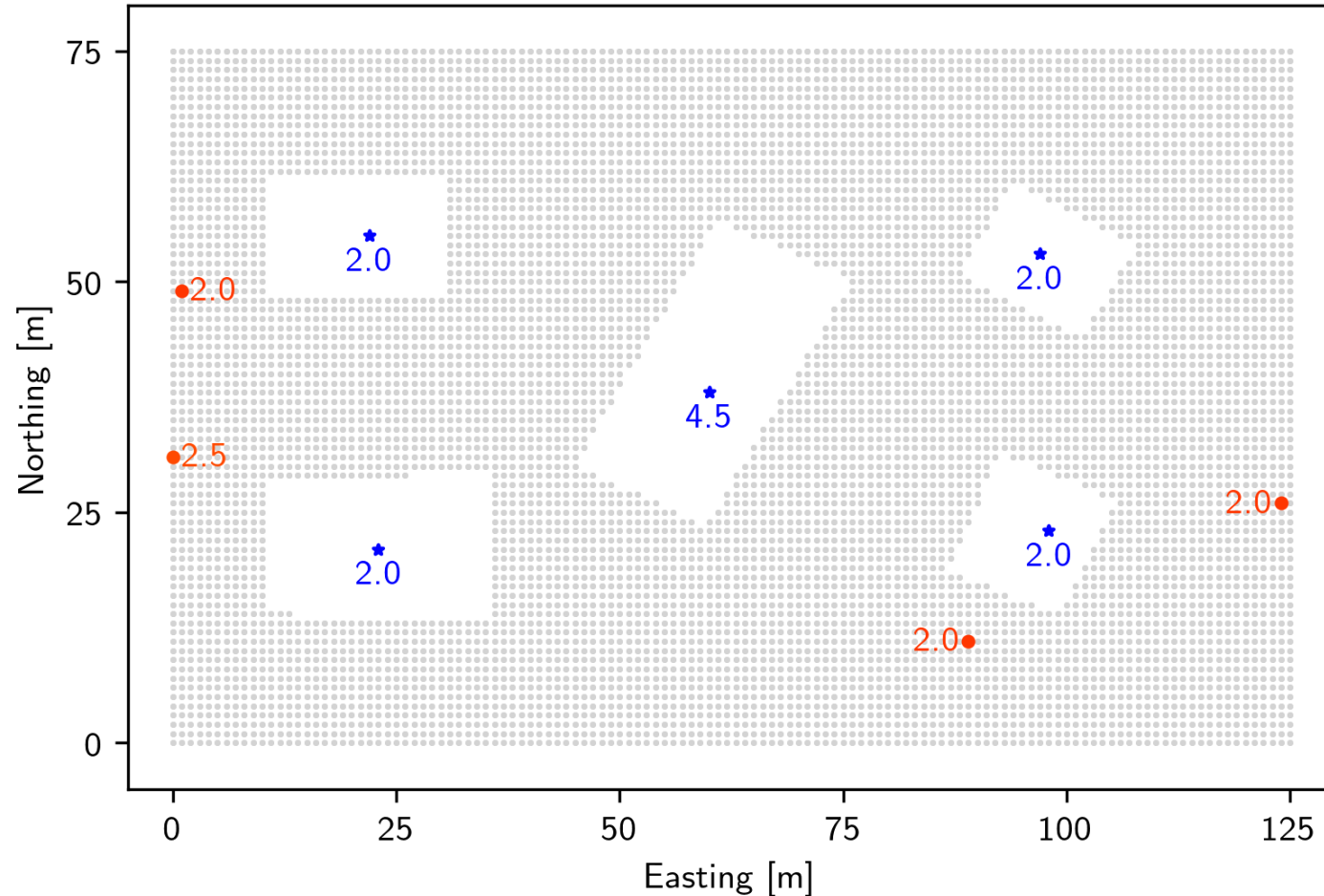
Best-3 sensor placement, coverage ratio = 0.75



- Possible sensor location
- Selected sensor location
- ★ Source location

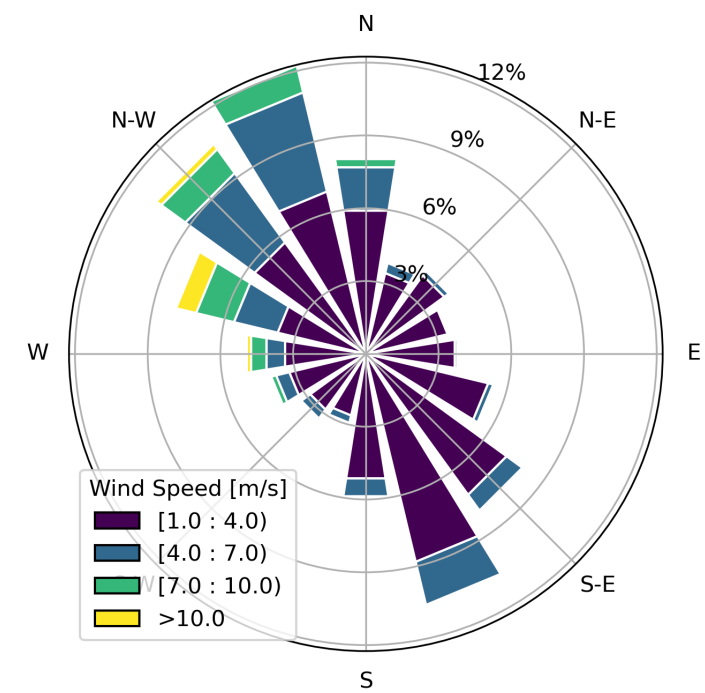
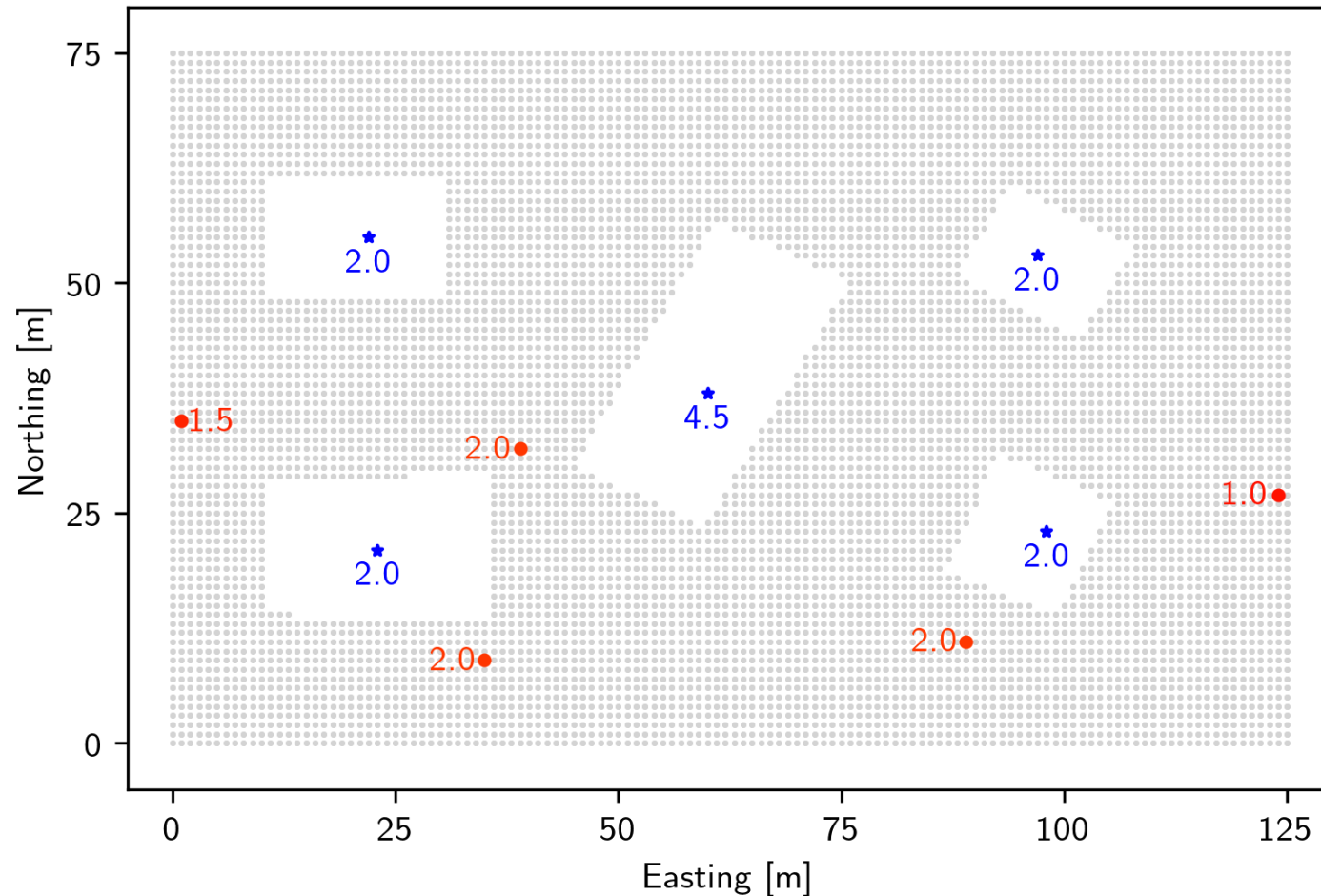
# Best-4 Sensor Placement

Best-4 sensor placement, coverage ratio = 0.82



# Best-5 Sensor Placement

Best-5 sensor placement, coverage ratio = 0.86

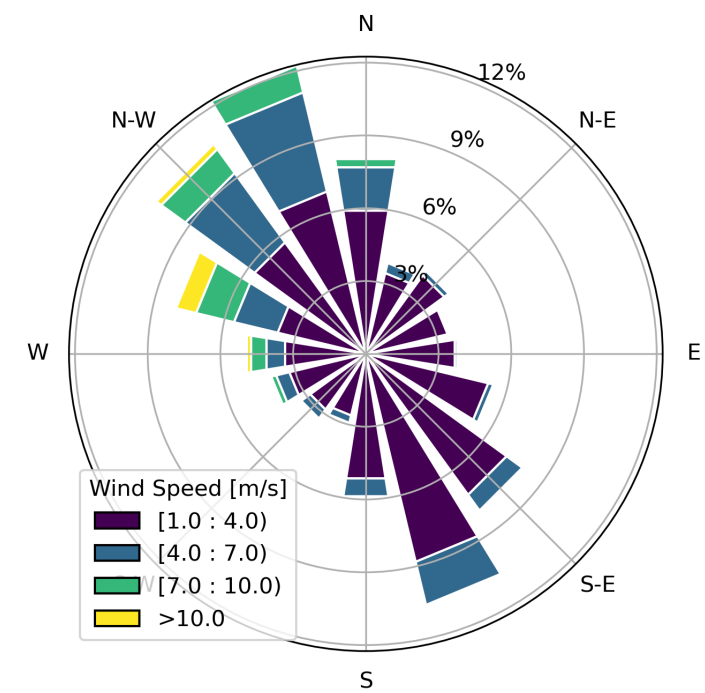
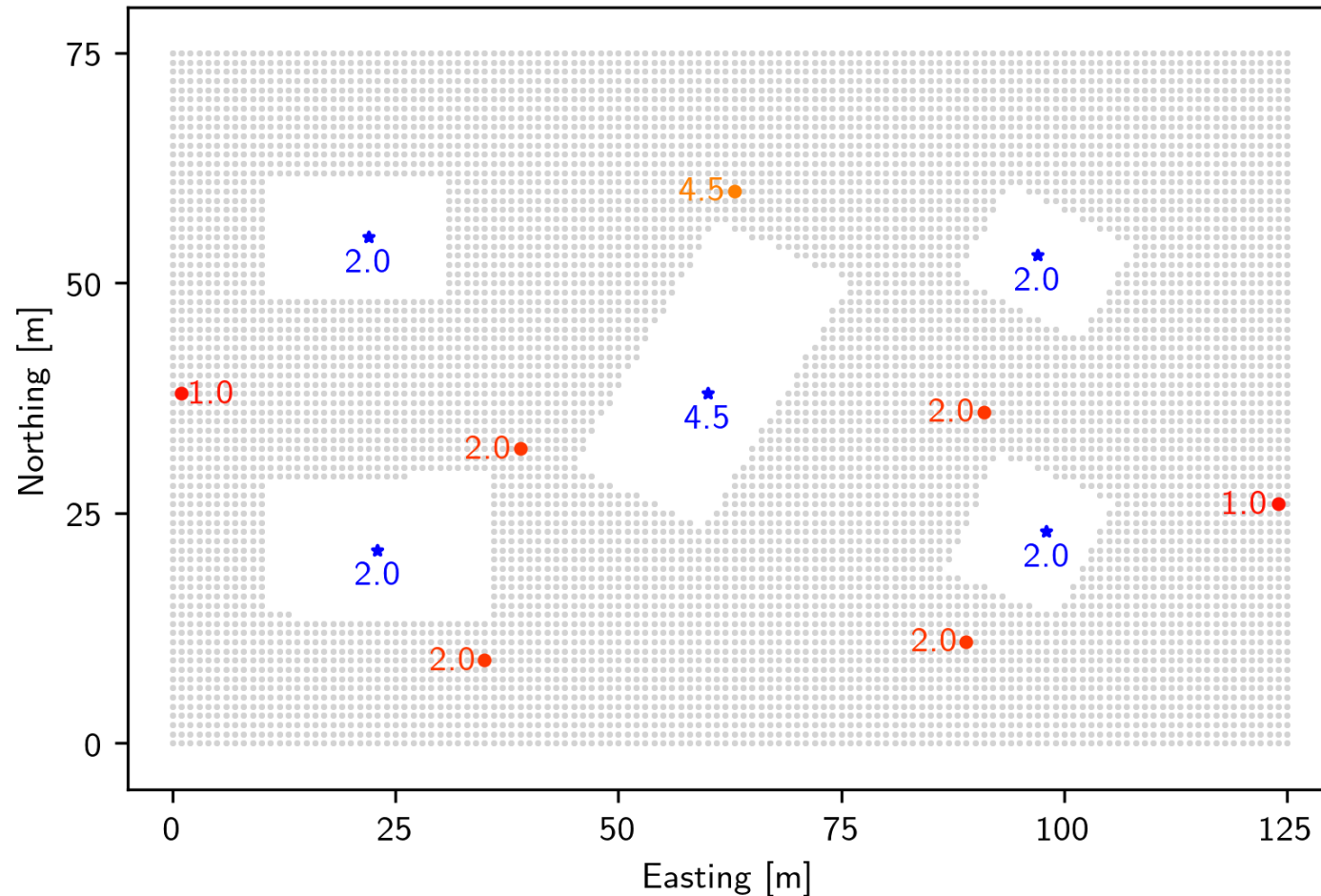


- Possible sensor location
- Selected sensor location
- ★ Source location



# Best-7 Sensor Placement

Best-7 sensor placement, coverage ratio = 0.92







# Best-10 Sensor Placement

Best-10 sensor placement, coverage ratio = 0.96

